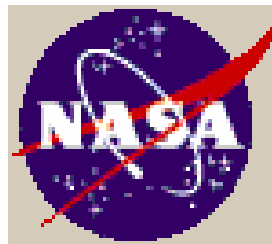


# PRECIPITATION DOWNSCALING: METHODOLOGIES AND HYDROLOGIC APPLICATIONS

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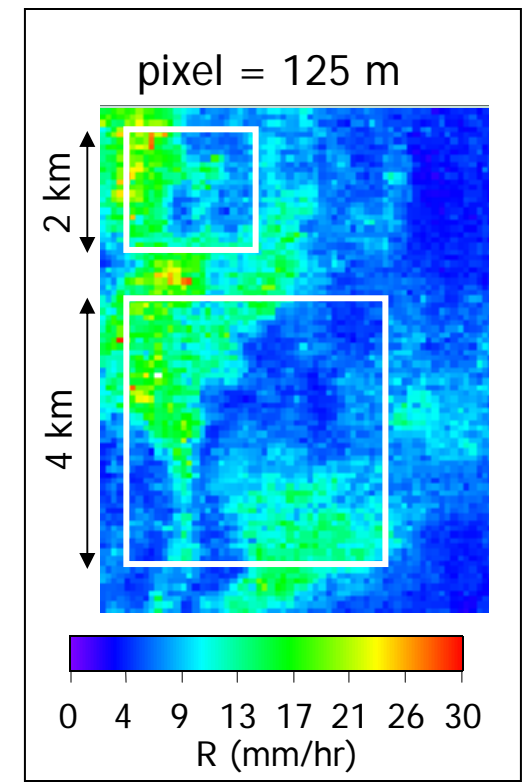
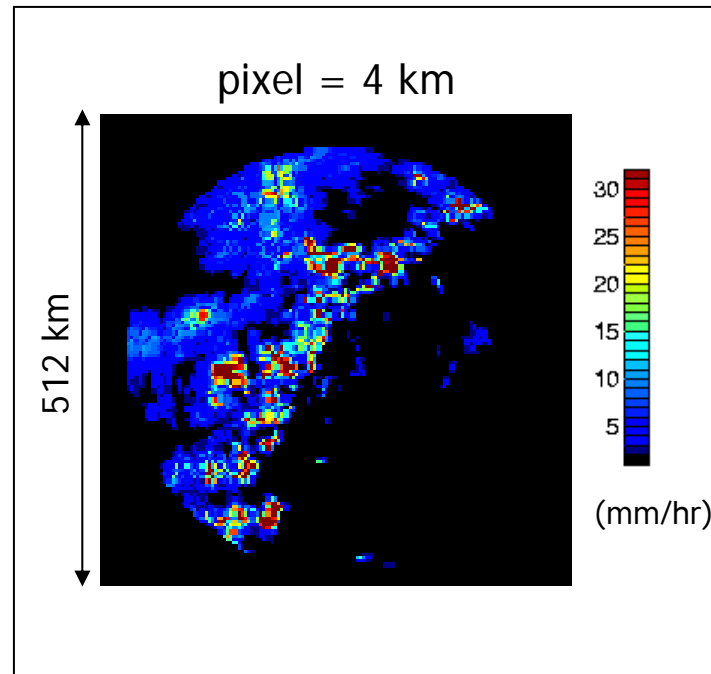
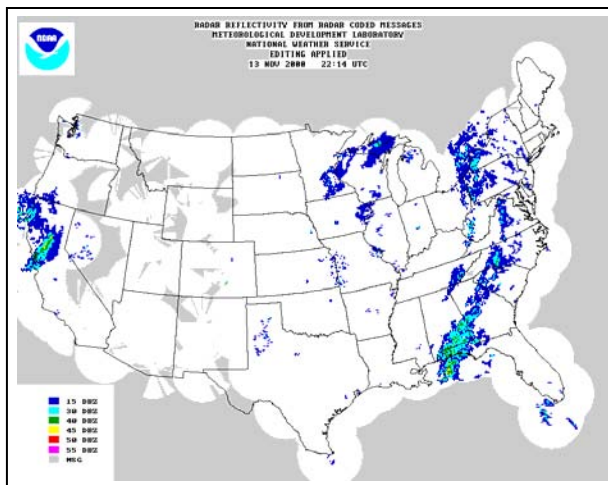
# DOWNSCALING

- ✓ **Downscaling** = "Creating" information at scales smaller than the available scales, or reconstructing variability at sub-grid scales. It is usually statistical in nature, i.e., statistical downscaling.
- ✓ Could be seen as equivalent to "**conditional simulation**" i.e, simulation conditional on preserving the statistics at the starting scale and/or other information.

# PREMISES OF STATISTICAL DOWNSCALING

- ✓ Precipitation exhibits space-time variability over a large range of scales (a few meters to thousand of Kms and a few seconds to several decades)
- ✓ There is a substantial evidence to suggest that despite the very complex patterns of precipitation, there is an underlying simpler structure which exhibits **scale-invariant statistical characteristics**
- ✓ If this scale invariance is unraveled and quantified, it can form the basis of moving up and down the scales: important for efficient and parsimonious downscaling methodologies

# Precipitation exhibits spatial variability at a large range of scales



# OUTLINE OF TALK

1. Multi-scale analysis of spatial precipitation
2. A spatial downscaling scheme
3. Relation of physical and statistical parameters for real-time or predictive downscaling
4. A space-time downscaling scheme
5. Hydrologic applications

# References

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6. Nykanen, D. and E. Foufoula-Georgiou, Soil moisture variability and its effect on scale-dependency of nonlinear parameterizations in coupled land-atmosphere models, *Advances in Water Resources*, 24(9-10), 1143-1157, doi: 10.1016/S0309-1708(01)00046-X, 2001.
7. Nykanen, D. K., E. Foufoula-Georgiou, and W. M. Lapenta, Impact of small-scale rainfall variability on larger-scale spatial organization of land-atmosphere fluxes, *J. Hydrometeor.*, 2, 105-120, doi: 10.1175/1525-7541(2001)002, 2001

# 1. Multiscale analysis - 1D example

$$\{x_1, x_2, x_3, x_4, x_5, x_6, x_7, x_8\}$$

$$\downarrow X_0 \equiv \bar{X}_0$$

$$\underbrace{\frac{x_1+x_2}{2} \quad \frac{x_3+x_4}{2} \quad \frac{x_5+x_6}{2} \quad \frac{x_7+x_8}{2}}_{\bar{X}_1}$$

$$\underbrace{\frac{x_1+x_2+x_3+x_4}{4} \quad \frac{x_5+x_6+x_7+x_8}{4}}_{\bar{X}_2}$$

$$\underbrace{\frac{x_1+x_2+x_3+x_4+x_5+x_6+x_7+x_8}{8}}_{\bar{X}_3}$$

# 1. Multiscale analysis - 1D example

$$\{x_1, x_2, x_3, x_4, x_5, x_6, x_7, x_8\}$$

$$X_0 \equiv \bar{X}_0$$

$$\underbrace{\frac{x_1+x_2}{2} \quad \frac{x_3+x_4}{2} \quad \frac{x_5+x_6}{2} \quad \frac{x_7+x_8}{2}}_{\bar{X}_1}$$

$$\underbrace{\frac{x_1-x_2}{2} \quad \frac{x_3-x_4}{2} \quad \frac{x_5-x_6}{2} \quad \frac{x_7-x_8}{2}}_{X'_1}$$

$$\underbrace{\frac{x_1+x_2+x_3+x_4}{4} \quad \frac{x_5+x_6+x_7+x_8}{4}}_{\bar{X}_2}$$

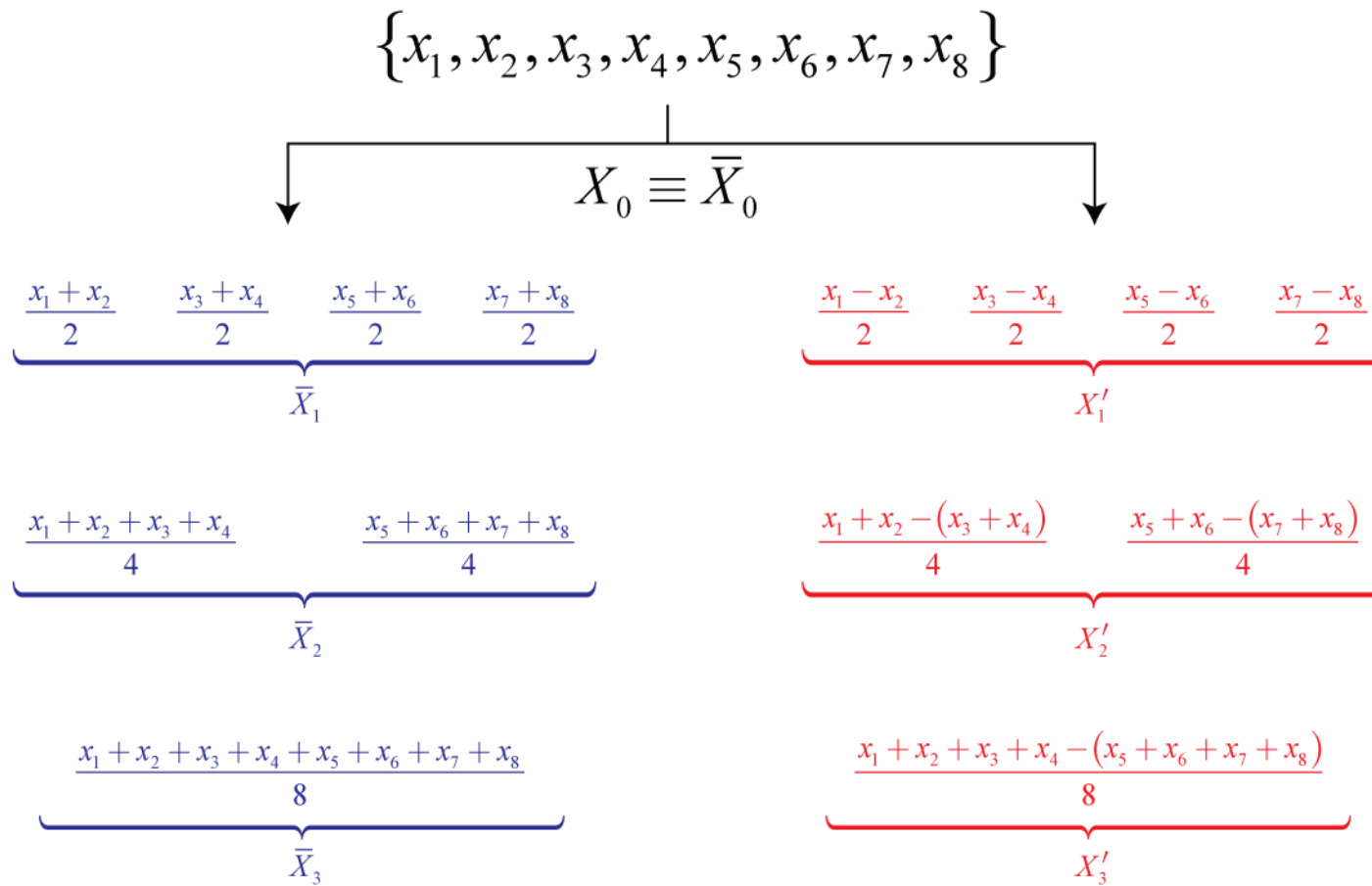
$$\underbrace{\frac{x_1+x_2-(x_3+x_4)}{4} \quad \frac{x_5+x_6-(x_7+x_8)}{4}}_{X'_2}$$

$$\underbrace{\frac{x_1+x_2+x_3+x_4+x_5+x_6+x_7+x_8}{8}}_{\bar{X}_3}$$

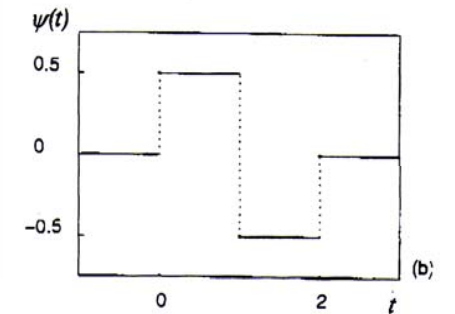
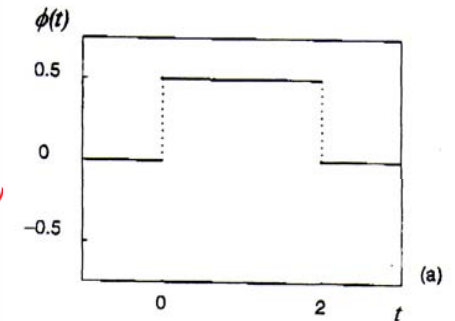
$$\underbrace{\frac{x_1+x_2+x_3+x_4-(x_5+x_6+x_7+x_8)}{8}}_{X'_3}$$



# 1. Multiscale analysis - 1D example



Haar Wavelet  
Multiscale Filter:

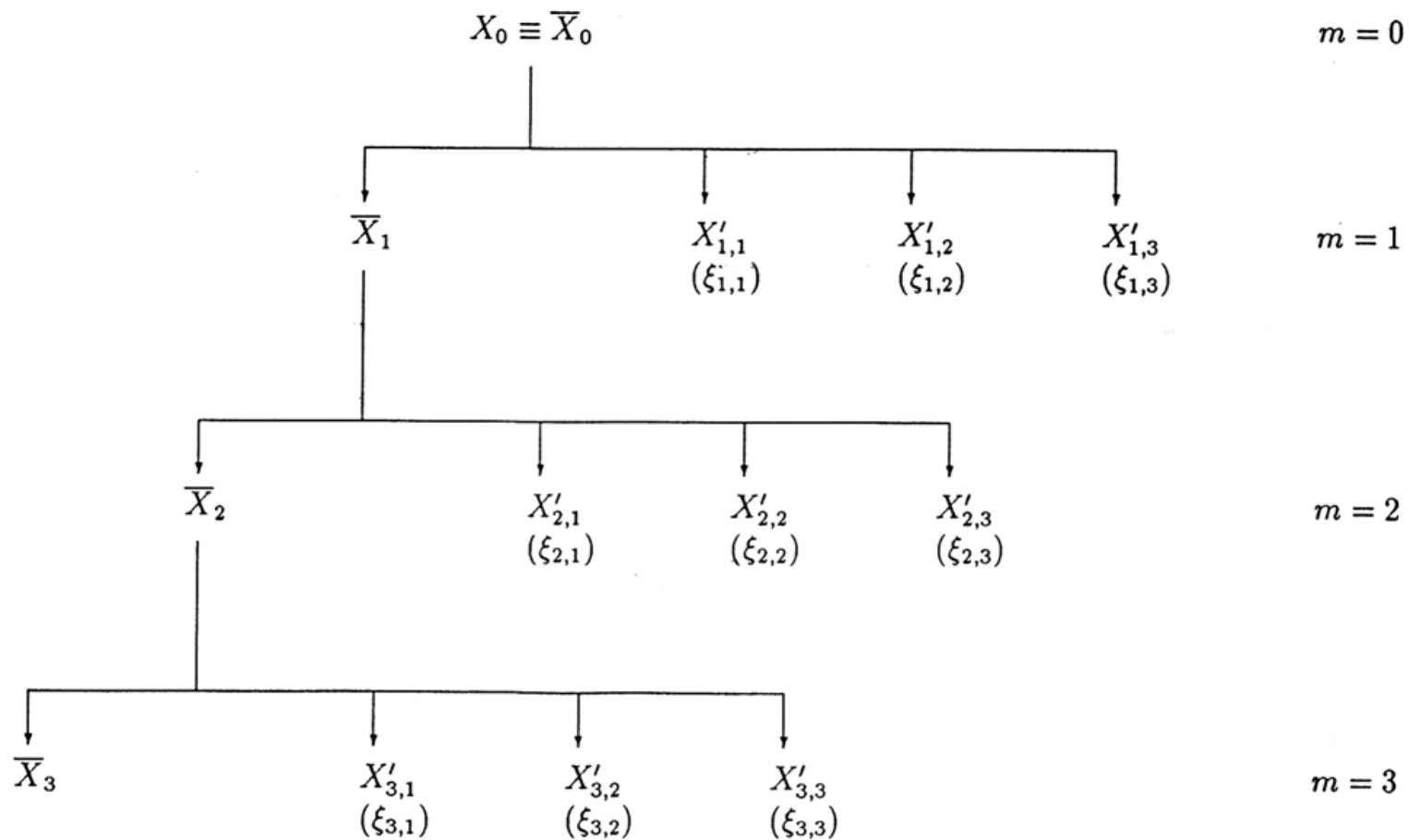


# Multiscale analysis via Wavelets

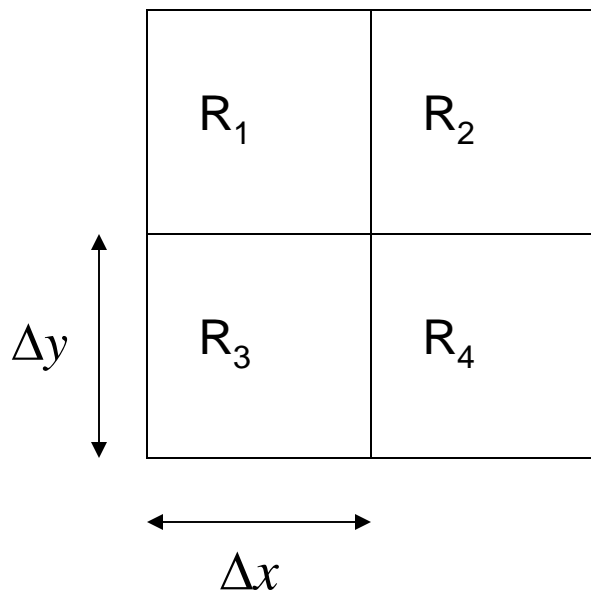
- ✓ Averaging and differencing at multiple scales can be done efficiently via a discrete orthogonal wavelet transform (WT), e.g., the Haar wavelet
- ✓ The inverse of this transform (IWT) allows efficient reconstruction of the signal at any scale given the large scale average and the "fluctuations" at all intermediate smaller scales
- ✓ It is easy to do this analysis in any dimension (1D, 2D or 3D).

(See Kumar and Foufoula-Georgiou, 1993)

# Multiscale analysis - 2D example



# Interpretation of directional fluctuations (gradients)

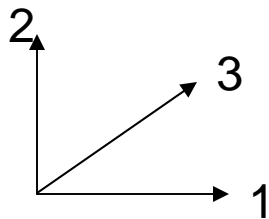


$$X'_1 = \frac{1}{2} \left[ \left( \frac{R_2 - R_1}{\Delta x} \right) + \left( \frac{R_4 - R_3}{\Delta x} \right) \right] \cong \frac{\partial R}{\partial x}$$

$$X'_2 = \frac{1}{2} \left[ \left( \frac{R_4 - R_2}{\Delta y} \right) + \left( \frac{R_3 - R_1}{\Delta y} \right) \right] \cong \frac{\partial R}{\partial y}$$

$$X'_3 = \frac{1}{2} \left[ \left( \frac{R_1 - R_4}{\Delta l} \right) + \left( \frac{R_2 - R_3}{\Delta l} \right) \right] \cong \frac{\partial^2 R}{\partial x \partial y}$$

$$\Delta l = \sqrt{\Delta x^2 + \Delta y^2}$$



(See Kumar and Foufoula-Georgiou, 1993)

# Observation 1

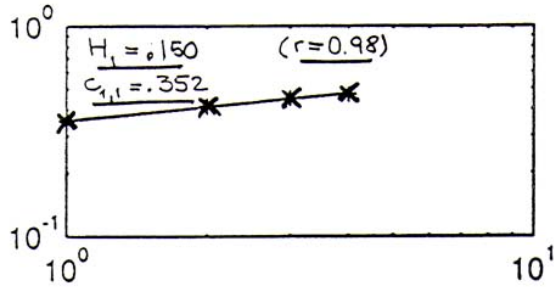
(See Perica and Foufoula-Georgiou, 1996)

- ✓ Local rainfall gradients (  $X'_{m,i=1,2,3}$  ) depend on local average rainfall intensities  $\bar{X}_m$  and were hard to parameterize
- ✓ But, standardized fluctuations  $\xi_{m,i=1,2,3} = \frac{X'_{m,i=1,2,3}}{\bar{X}_m}$ 
  - are approximately independent of local averages
  - obey approximately a Normal distribution centered around zero, i.e, have only 1 parameter to worry about in each direction

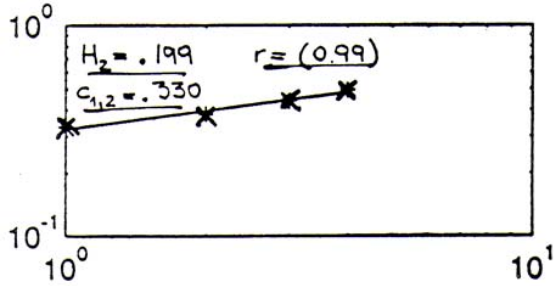
At scale m:  $\sigma_{\xi_1}$  ,  $\sigma_{\xi_2}$  ,  $\sigma_{\xi_3}$

# Observation 2

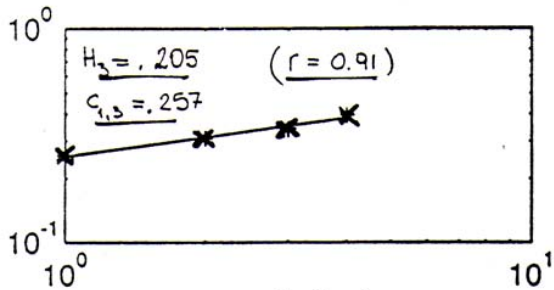
$\sigma_{\xi_1}$  :



$\sigma_{\xi_2}$  :

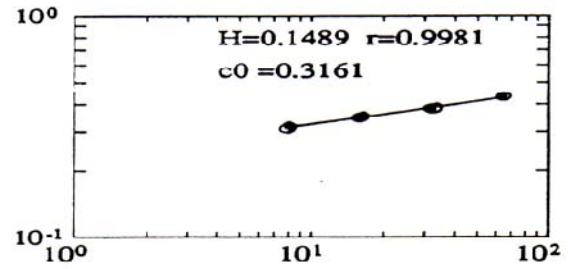
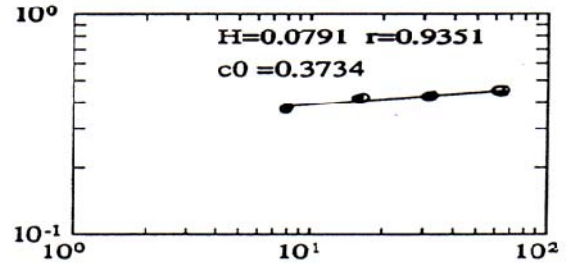
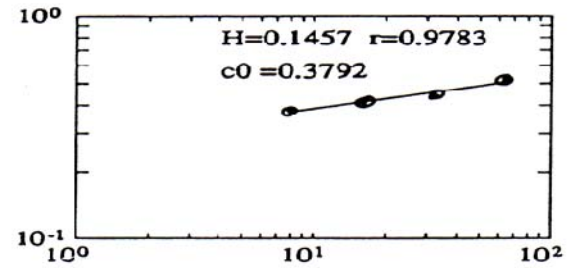


$\sigma_{\xi_3}$  :



May 13, 1985, 1248 UTC

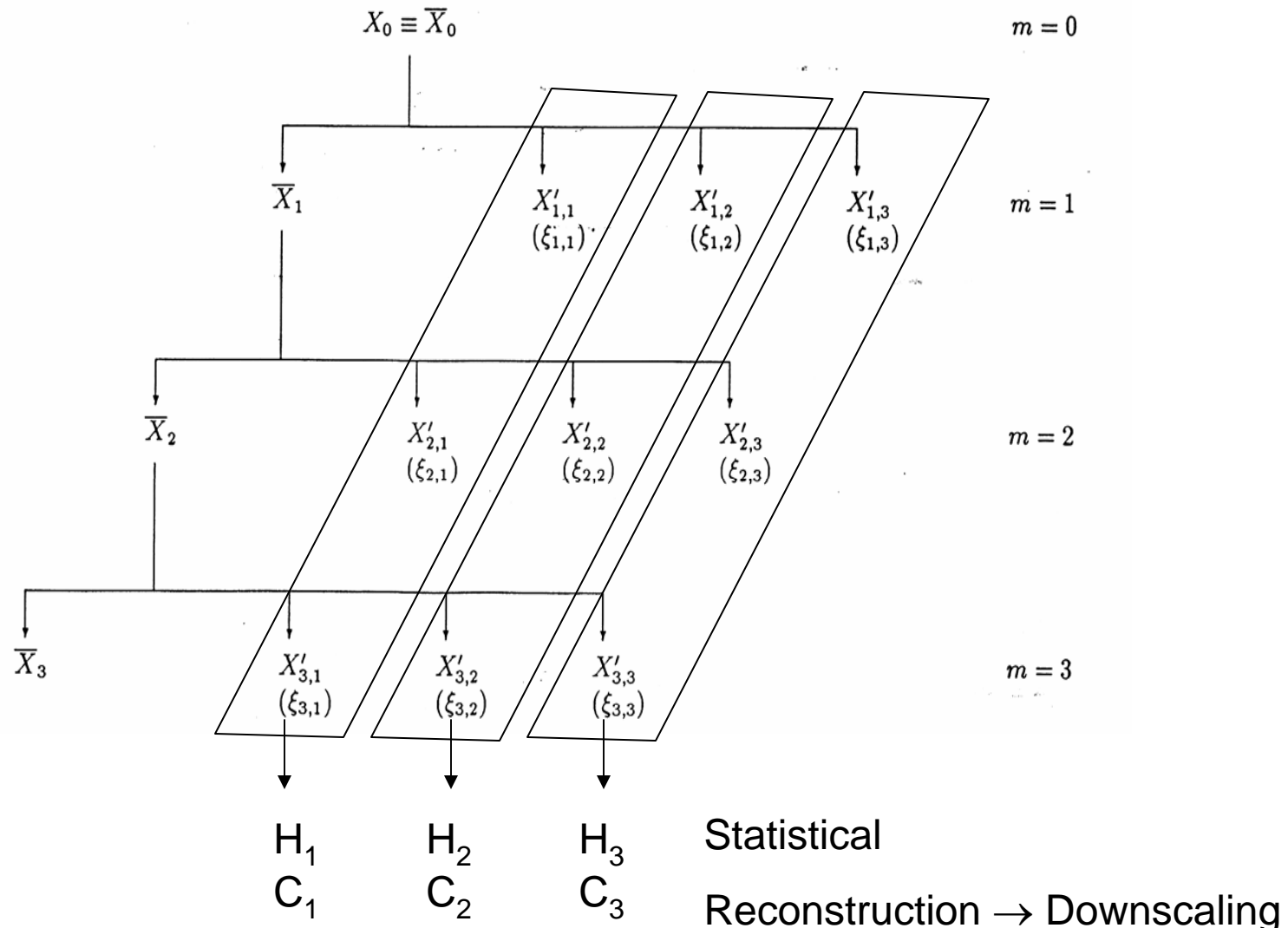
scale coefficient - c



June 11, 1985, 0300 UTC

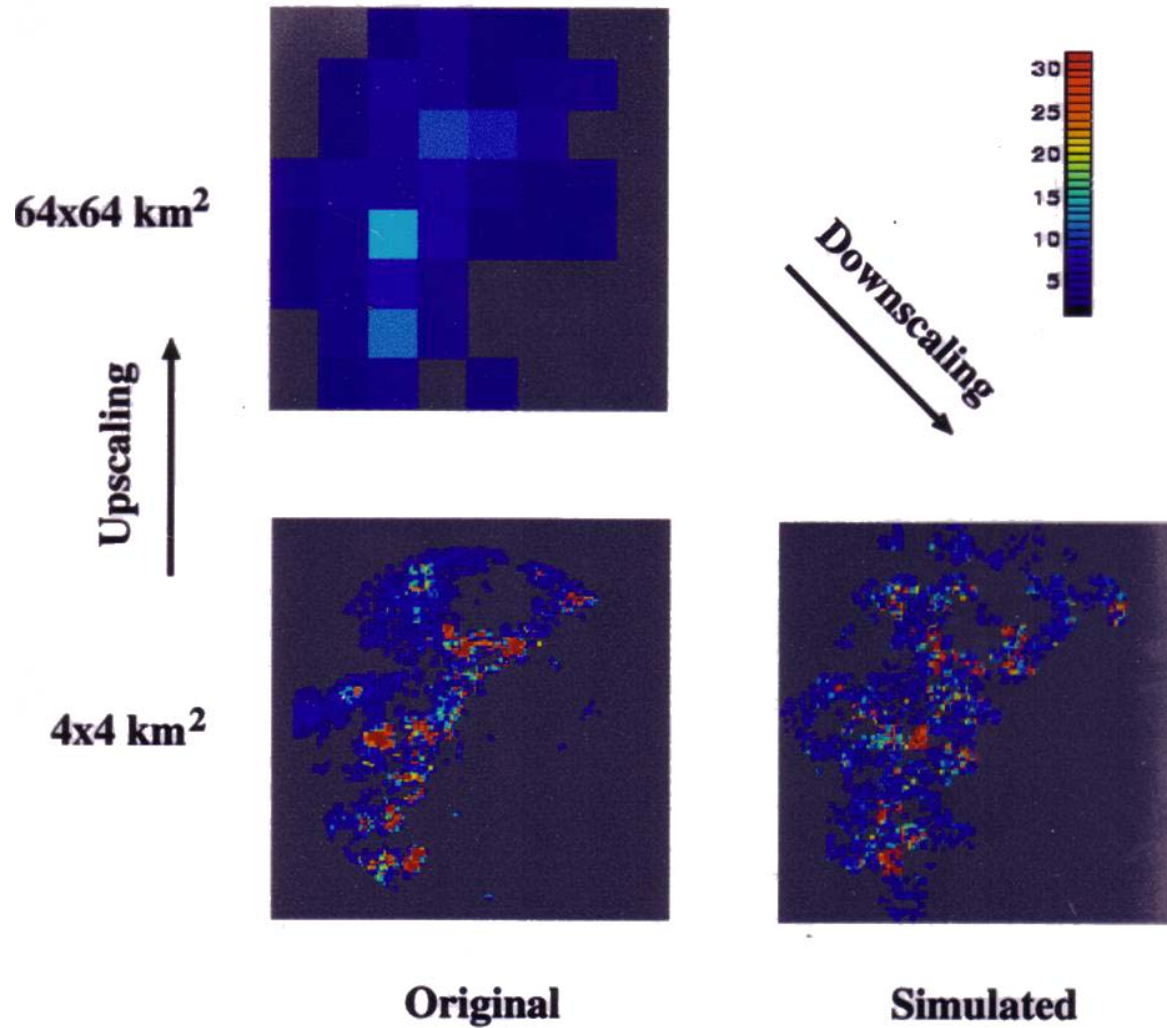
(See Perica and Foufoula-Georgiou, 1996)

## 2. Spatial downscaling scheme



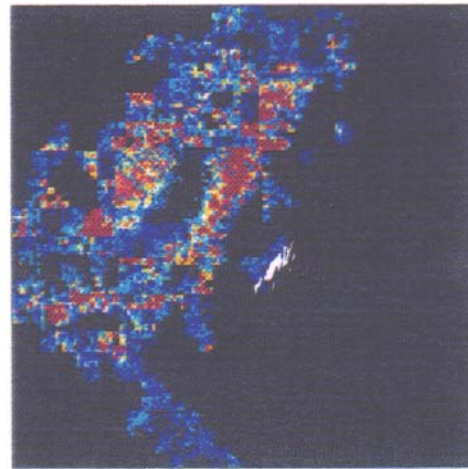
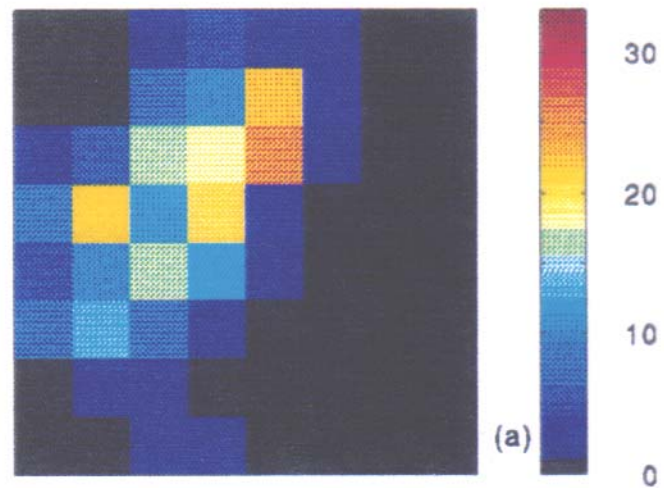
(See Perica and Foufoula-Georgiou, 1996)

# Example of downscaling

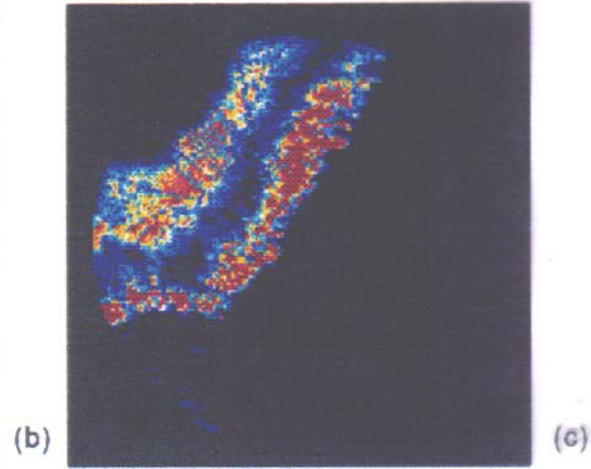




# Example of downscaling

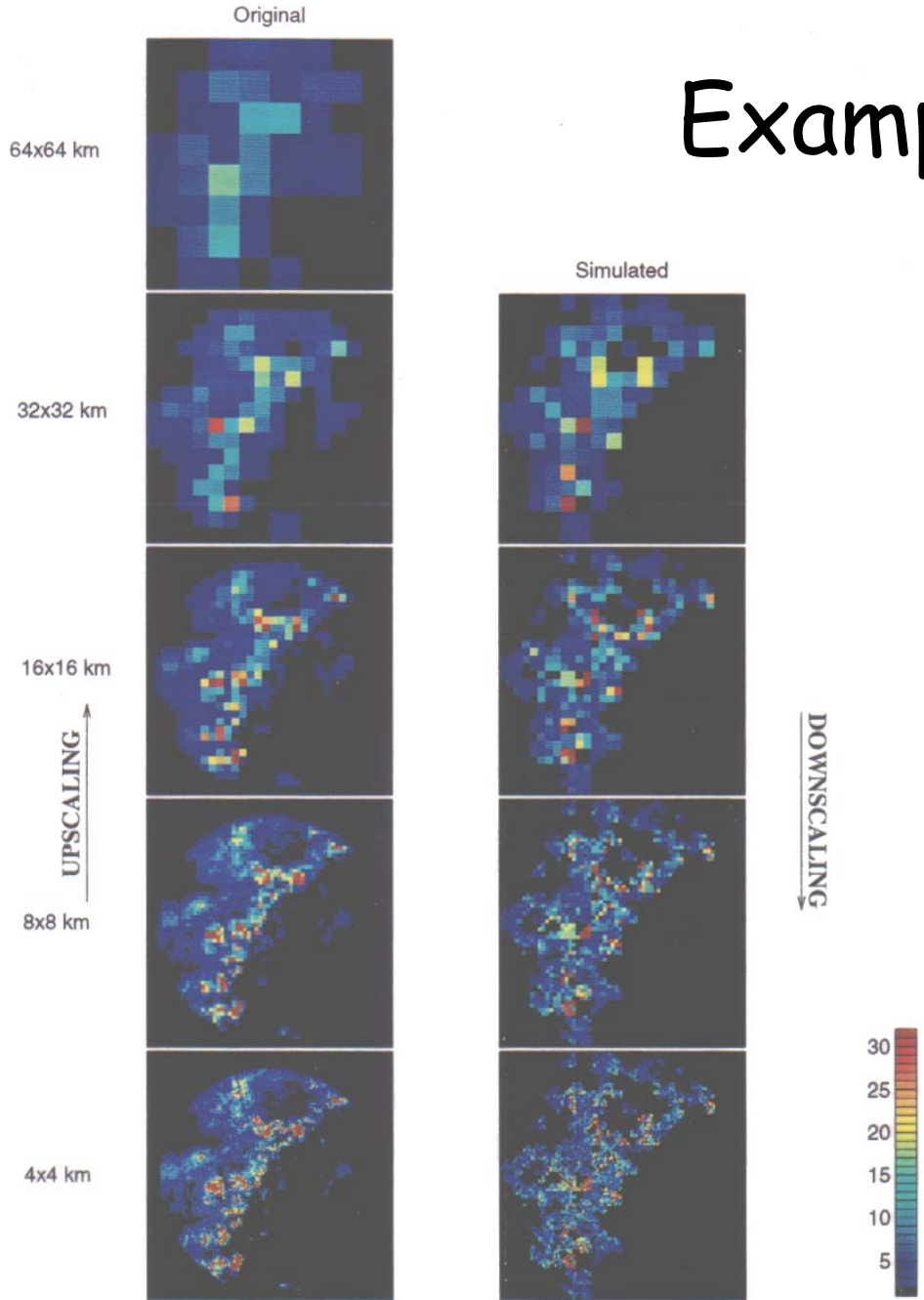


DOWNSCALED



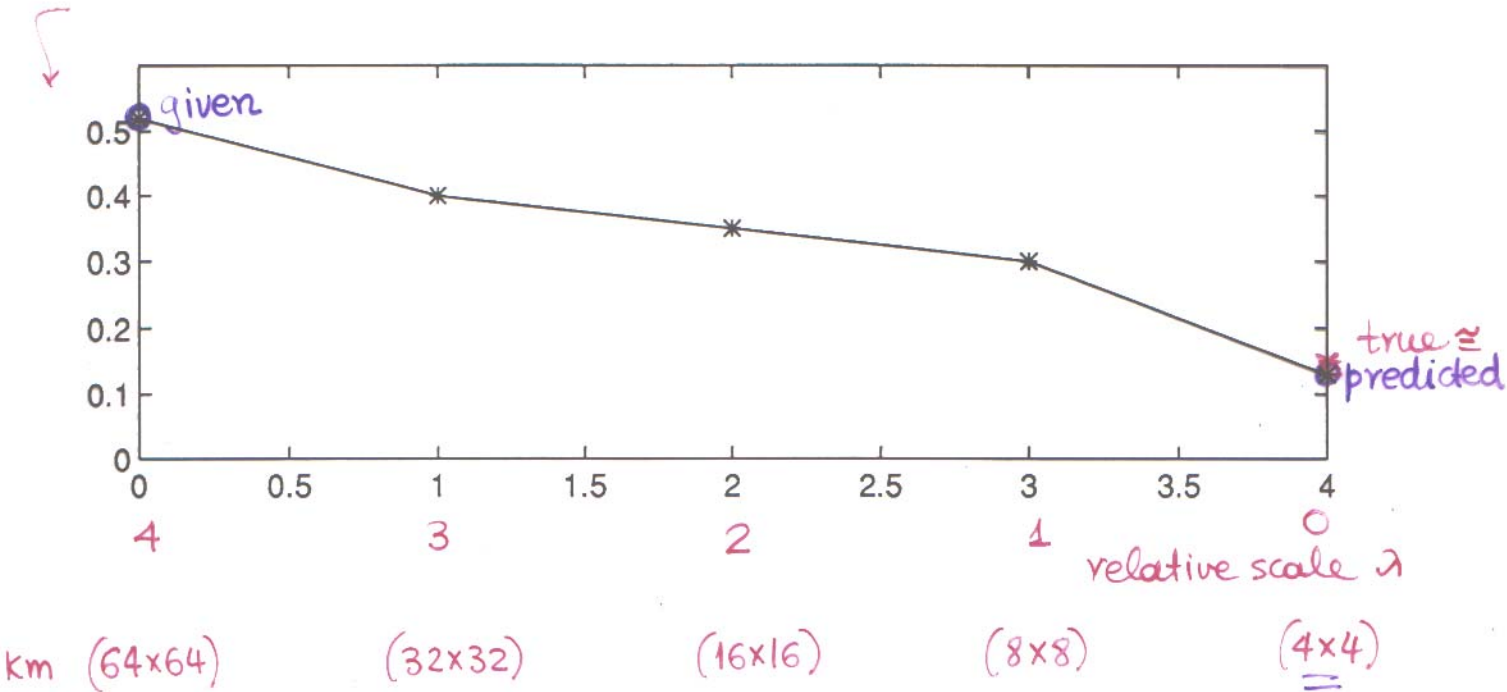
REAL

# Example of downscaling

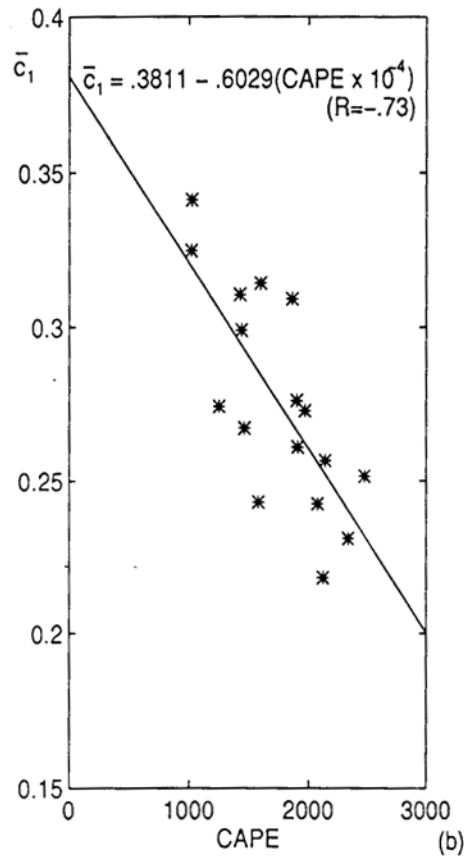
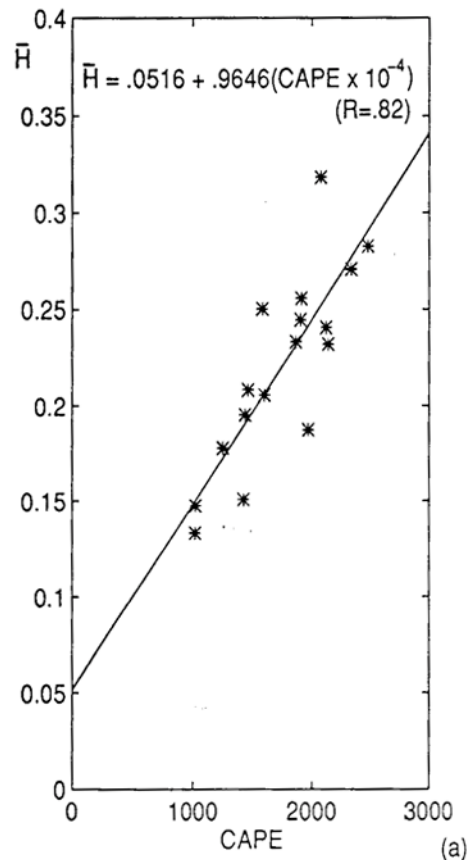


# Performance of downscaling scheme

fraction of area covered by rain



# 3. Relation of statistical parameters to physical observables



DEFINITION OF CAPE ( $\text{m}^2/\text{sec}^2$ )

$$\text{CAPE} = \int_{\text{LFC}}^{\text{EL}} g \cdot \left( \frac{\theta_c - \theta_{\text{env}}}{\theta_{\text{env}}} \right) dz$$

$\theta_c$  = potential T of an air parcel lifted from the surface to the level  $z$

$\theta_{\text{env}}$  = potential T of the unsaturated environment at the same level

LFC = level of free convection

EL = equilibrium level

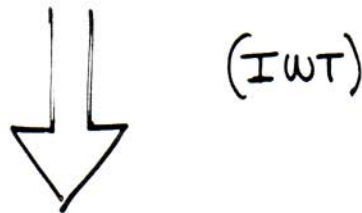
▷ CAPE is a measure of the potential instability

(See Perica and Foufoula-Georgiou, 1996)

# Predictive downscaling

## Given

- large scale mean (e.g. 64x64 km average rain)
- prestorm environmental conditions (CAPE)
- parameters of predictive eqns  $(CAPE, \bar{H})$ ,  $(CAPE, \bar{Q})$

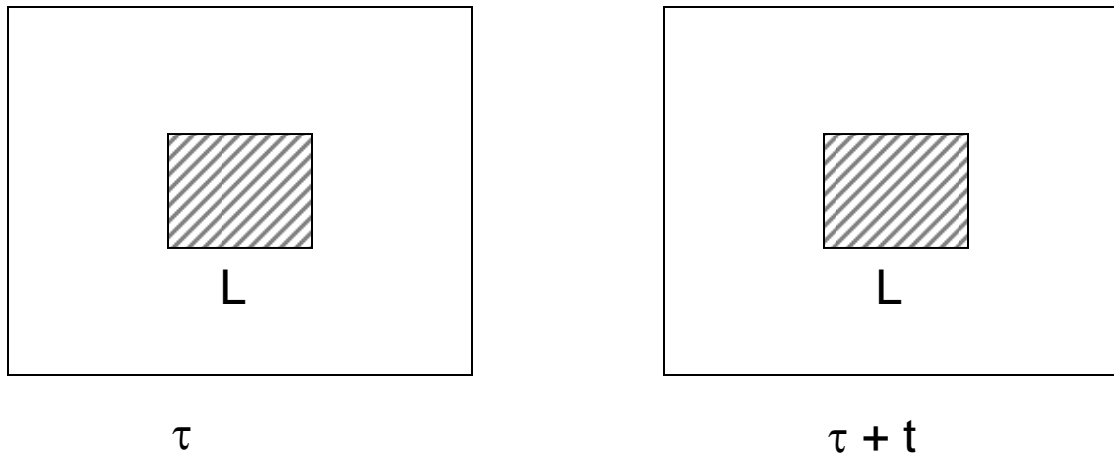


## Find

- rainfall at any smaller scale

# 4. Space-time Downscaling

- ✓ Describe rainfall variability at several spatial and temporal scales
- ✓ Explore whether space-time scale invariance is present. Look at rainfall fields at times  $\tau$  and  $(\tau+t)$ .



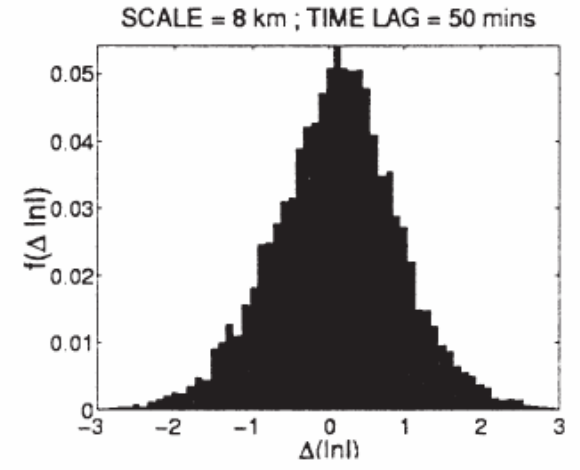
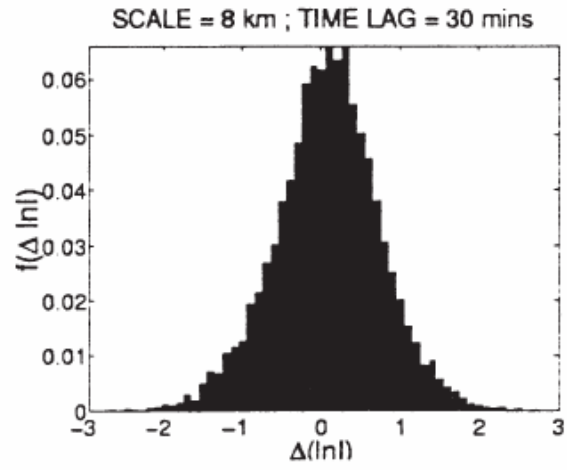
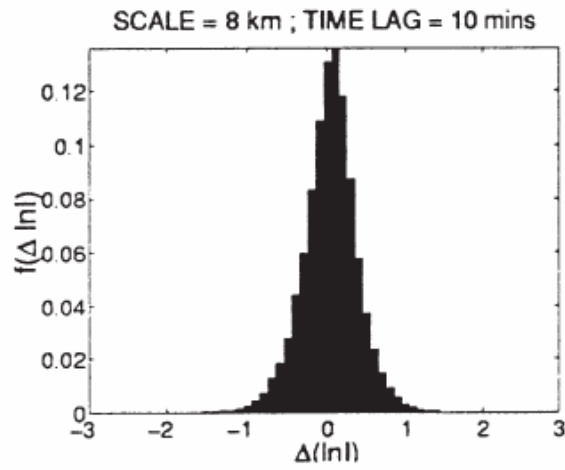
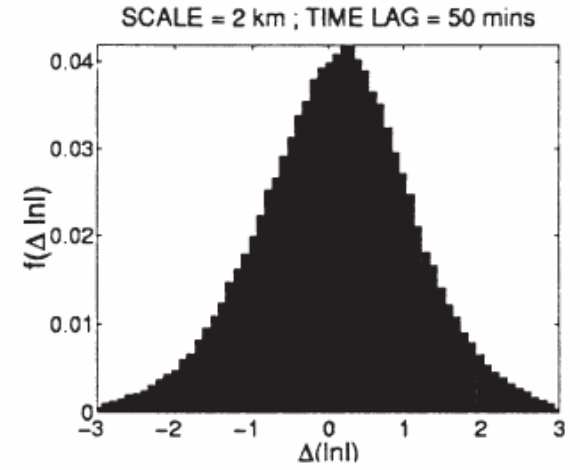
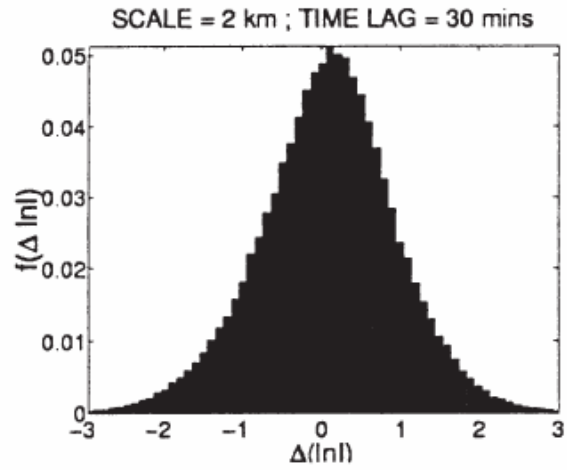
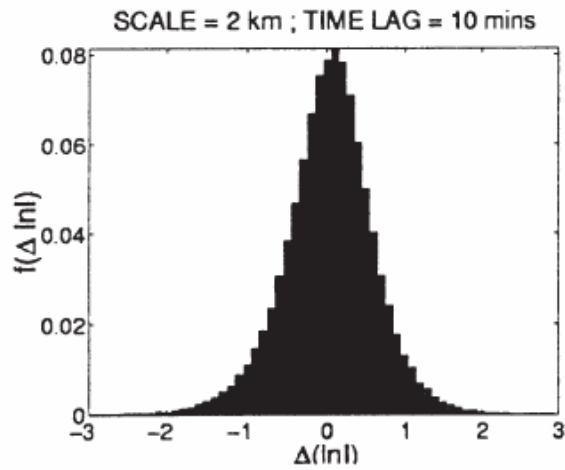
- ✓ Change  $L$  and  $t$  and compute statistics of evolving field

$$\Delta I(t, L) = I(\tau + t, L) - I(\tau, L)$$

$$\frac{\Delta I}{I}(t, L) = \frac{I(\tau + t, L) - I(\tau, L)}{\frac{1}{2} [I(\tau + t, L) + I(\tau, L)]}$$

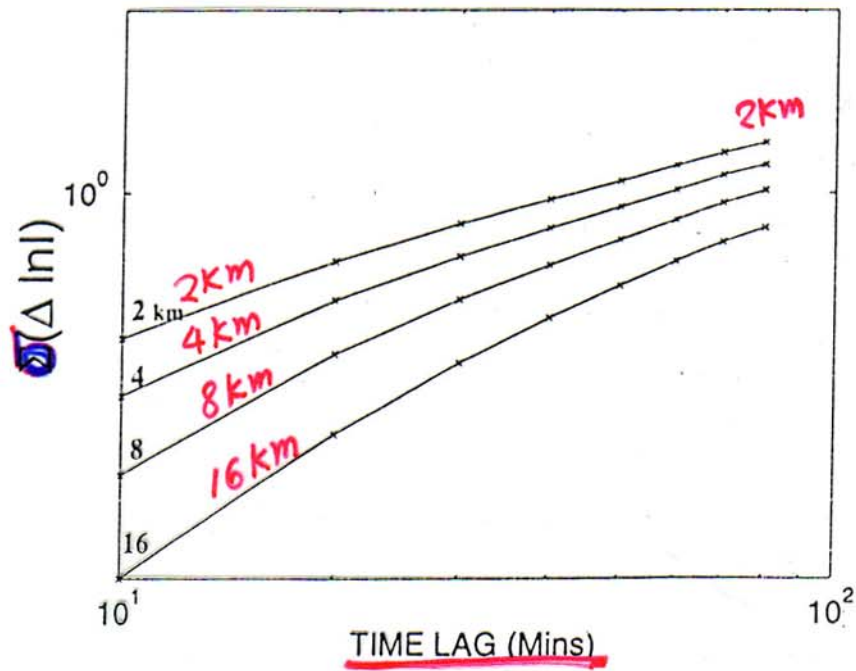
→  $\Delta \ln I(t, L)$

# PDFs of $\Delta \ln I$

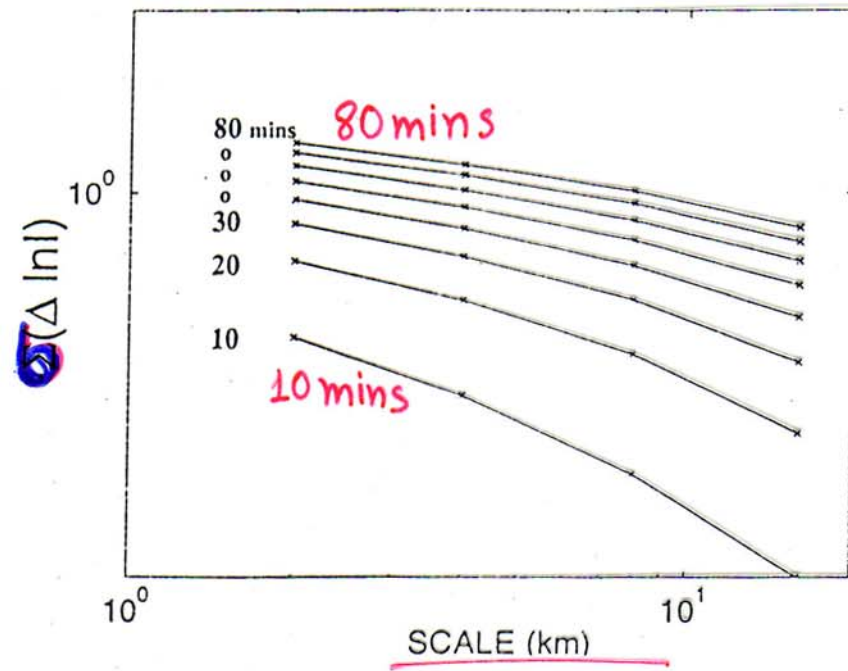


# $\sigma(\Delta \ln I)$ vs. Time Lag and vs. Scale

(a)



(b)





# Space-time scaling

- ✓ **Question:** Is it possible to rescale space and time such that some scale-invariance is unraveled?
- ✓ Look for transformation that relate the dimensionless quantities  $(t_1 / t_2)$  and  $(L_1 / L_2)$
- ✓ Possible only via transformation of the form  $t \sim L^z$  : "Dynamic scaling"

# Variance of $\Delta \ln I(t,L)$

		Time Lag $t$ (min)							
		10	20	30	40	50	60	70	80
$L$ (km)	2	0.58	0.77	0.89	0.97	1.05	1.11	1.17	1.21
	4	0.47	0.67	0.79	0.87	0.95	1.01	1.07	1.12
	8	0.35	0.55	0.67	0.76	0.84	0.90	0.96	1.01
	16	0.23	0.40	0.53	0.63	0.71	0.77	0.83	0.88



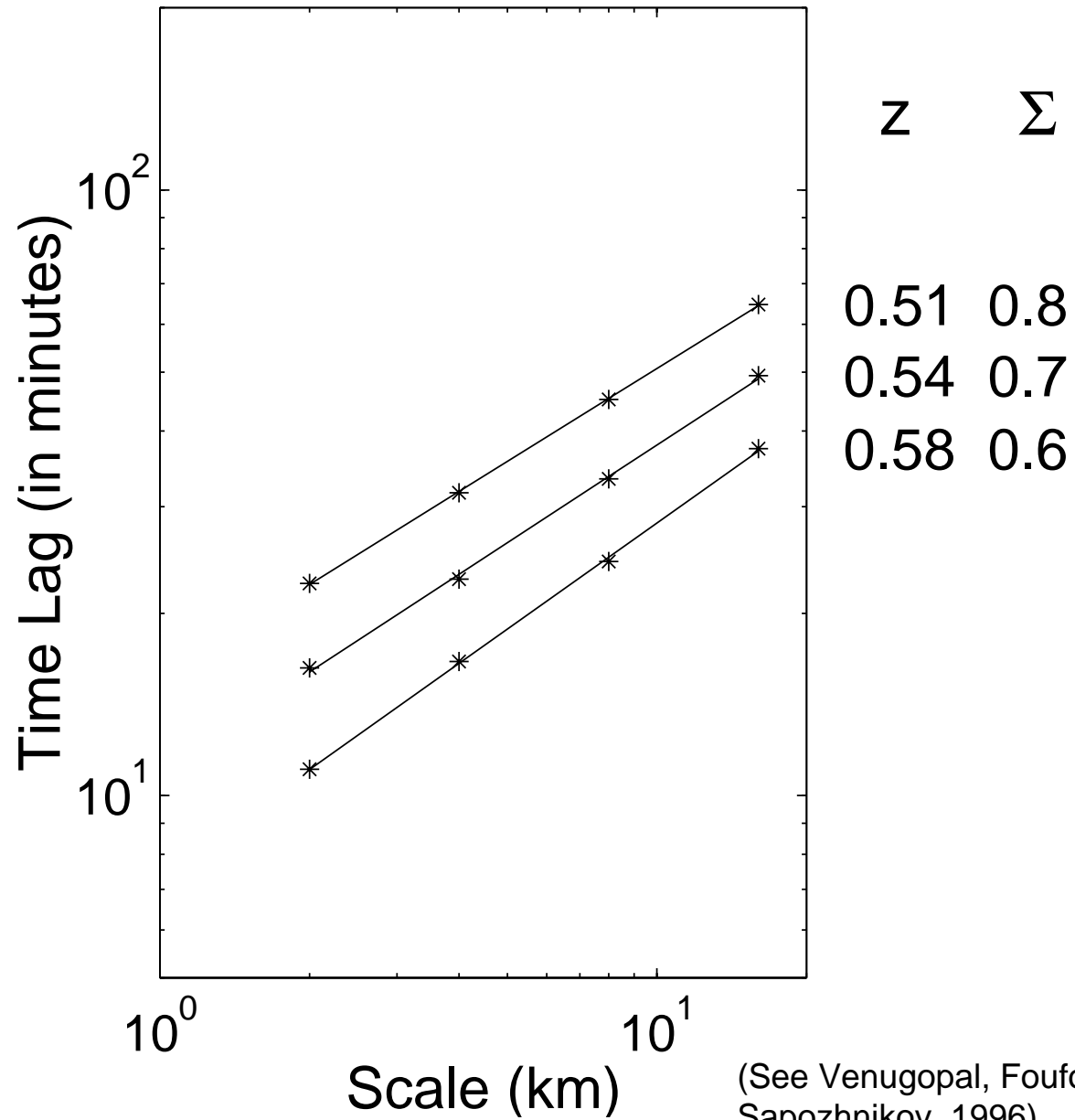
Find  $(t,L)$  pairs for which  $\text{var}(\Delta \ln I) = \text{constant}$



$$\text{var}(\Delta \ln I) = \sum (\Delta \ln I)$$

		0.6	0.7	0.8
$L$ (km)	2	11.1	16.3	22.4
	4	16.6	22.8	31.6
	8	24.4	33.3	45.1
	16	37.4	49.4	64.7

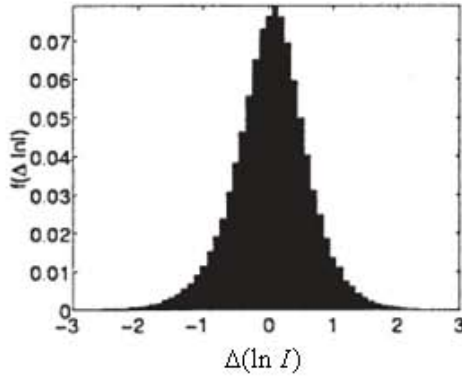
Dec. 28, 1993 : Iso- $\Sigma(\Delta \ln I)$  Lines



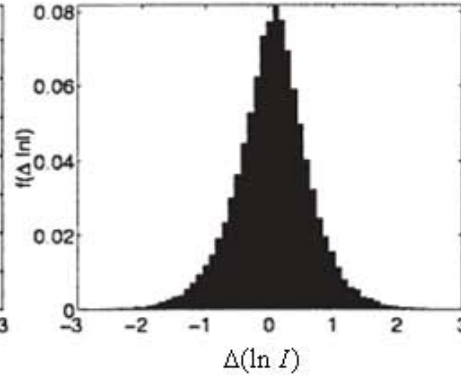
(See Venugopal, Foufoula-Georgiou and Sapozhnikov, 1996)

$$\sum(\Delta \ln I) = 0.6, z = 0.58$$

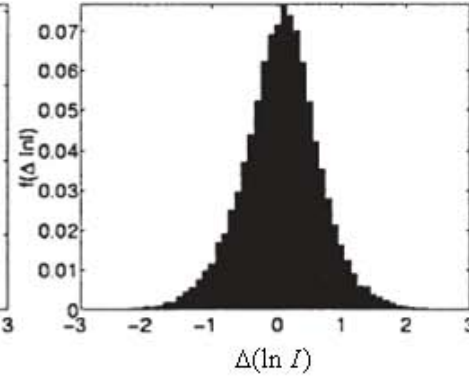
$L = 2\text{km} ; T = 11.1\text{ mins}$



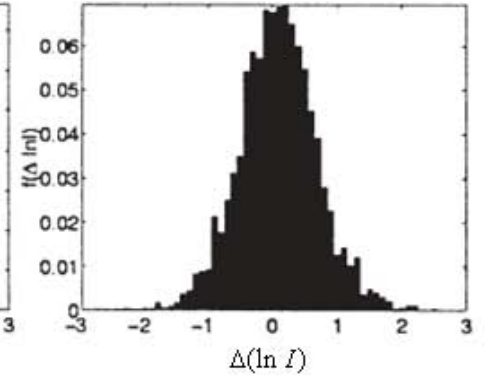
$L = 4\text{km} ; T = 16.6\text{ mins}$



$L = 8\text{km} ; T = 24.4\text{ mins}$

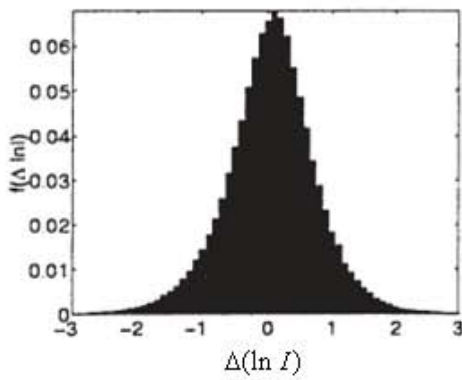


$L = 16\text{km} ; T = 37.4\text{ mins}$

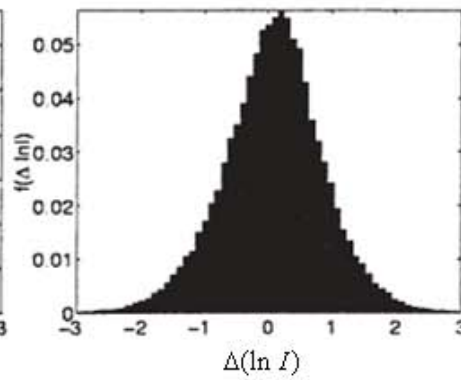


$$\sum(\Delta \ln I) = 0.8, z = 0.58$$

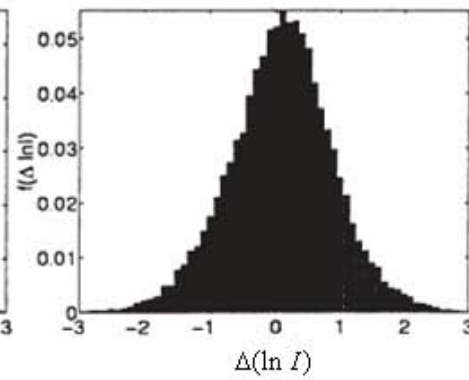
$L = 2\text{km} ; T = 16.3\text{ mins}$



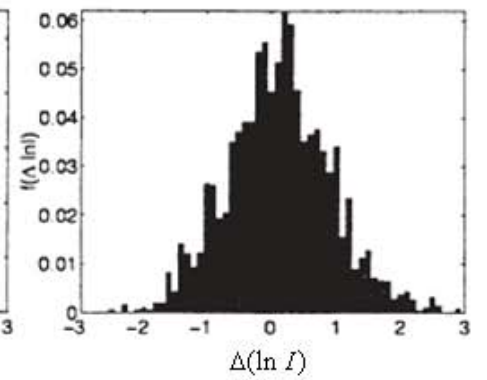
$L = 4\text{km} ; T = 31.6\text{ mins}$



$L = 8\text{km} ; T = 45.1\text{ mins}$



$L = 16\text{km} ; T = 64.7\text{ mins}$



## What do these values of $z$ mean?

Consider for instance,  $z = 0.6$ ,

Dynamic scaling implies

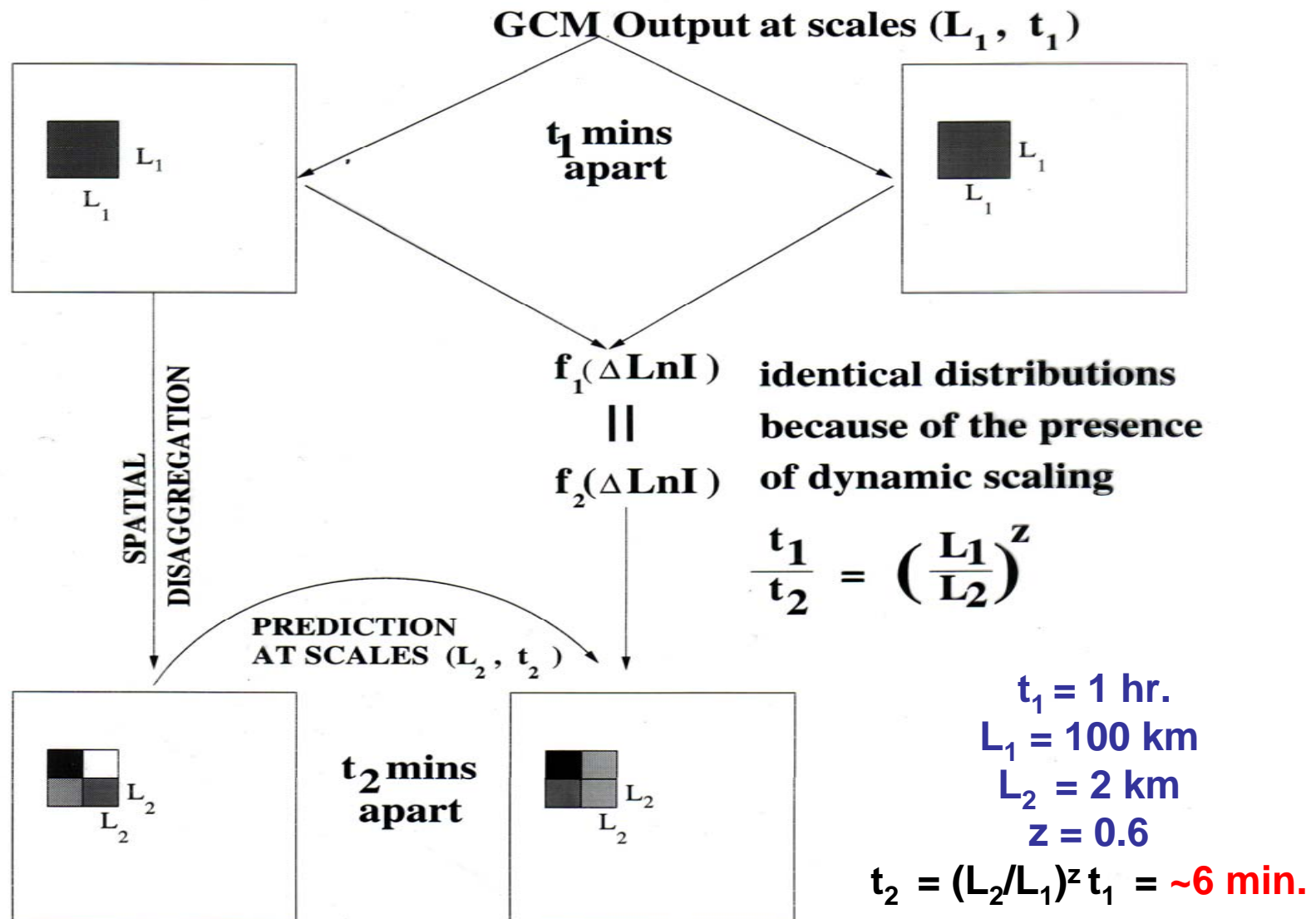
$$(t_1/t_2) = (L_1/L_2)^z$$

$\implies$  A feature **eight times** smaller will evolve **3 times** faster than the larger feature.

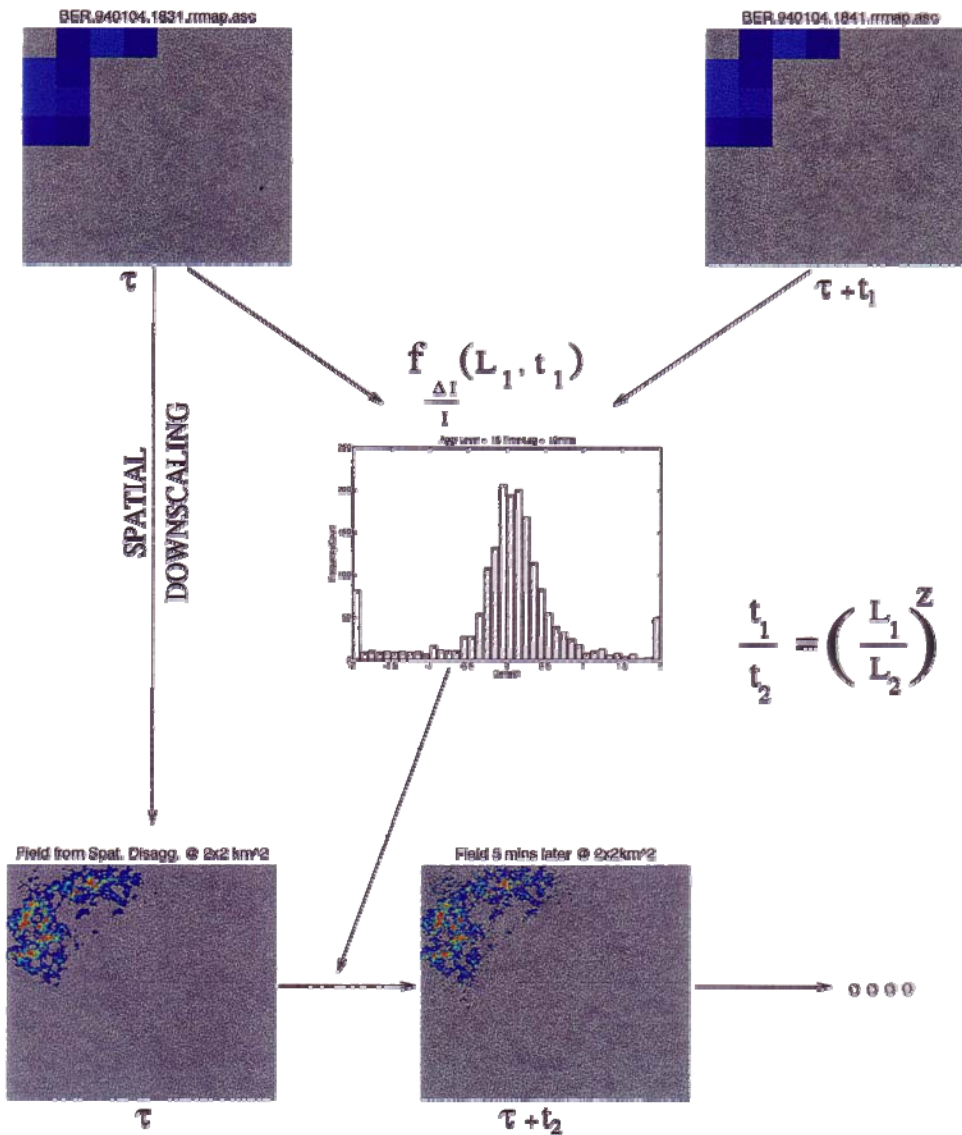
since

$$t_2 = t_1 \left(\frac{16}{2}\right)^{0.6} \approx 3t_1$$

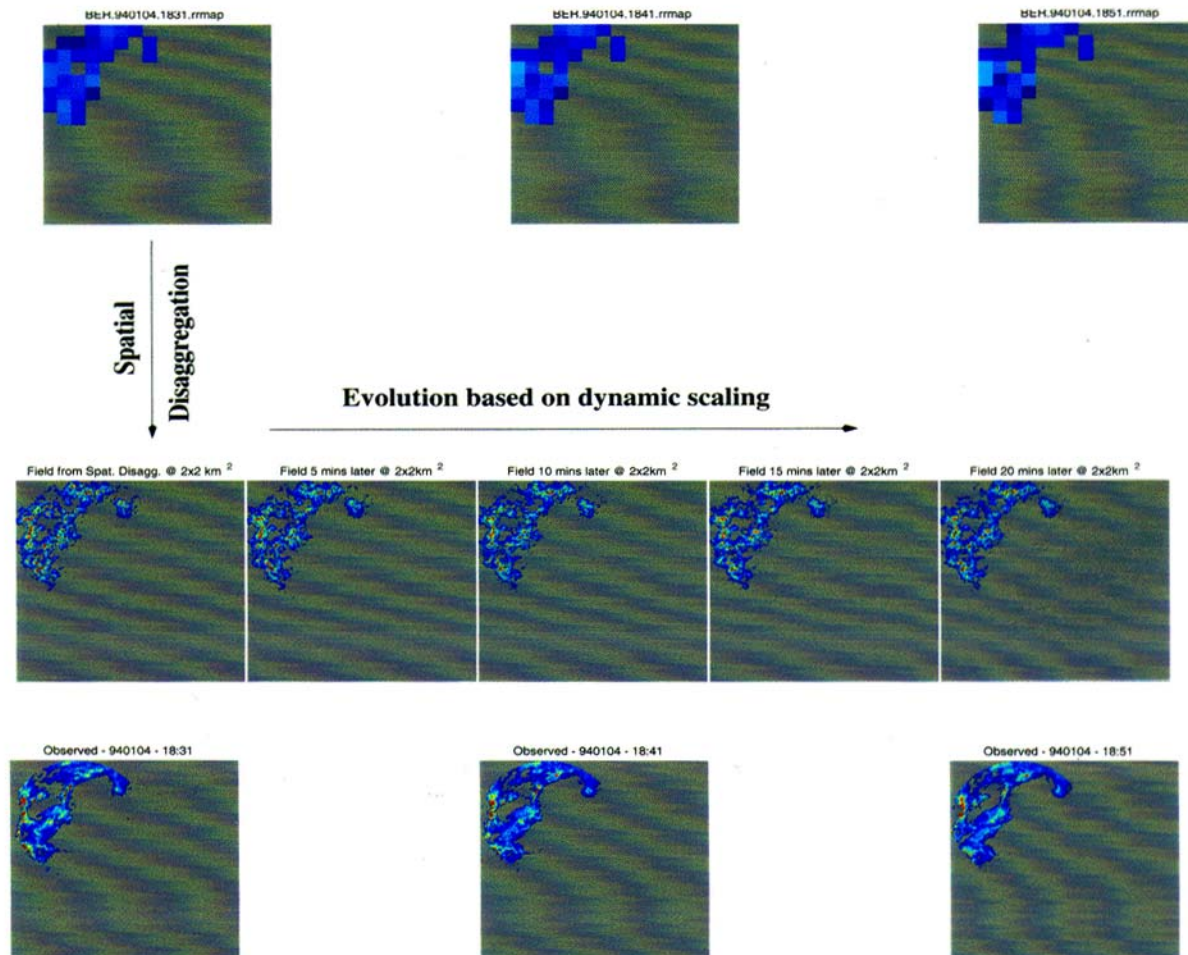
# Schematic of space-time downscaling



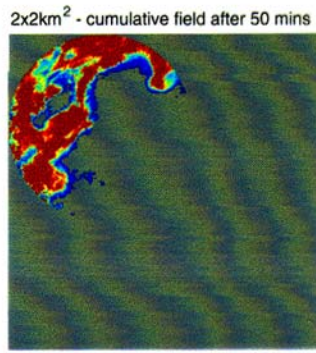
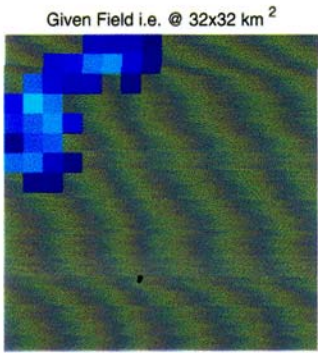
# Schematic of space-time downscaling



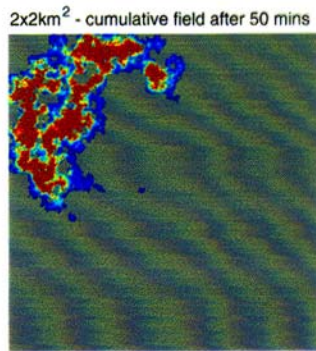
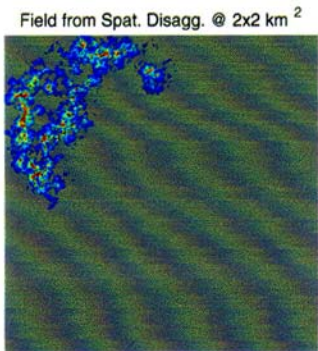
# Space-time Downscaling preserves temporal persistence



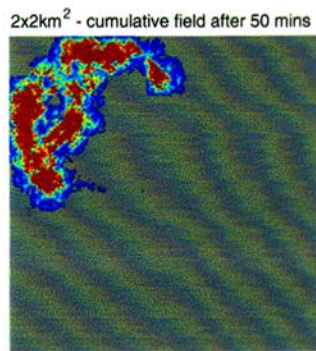




Observed

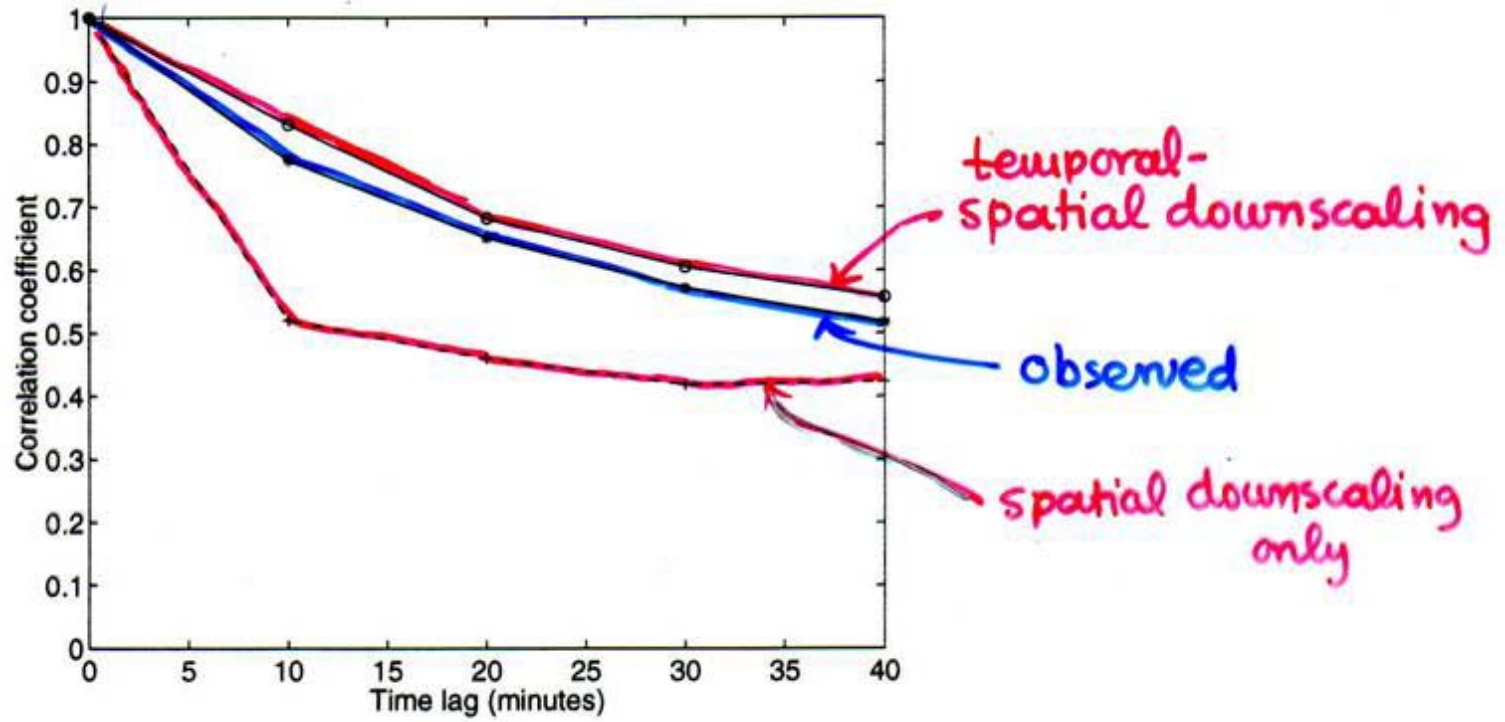


Accumulation of spatially  
downscaled field (every 10  
minutes)

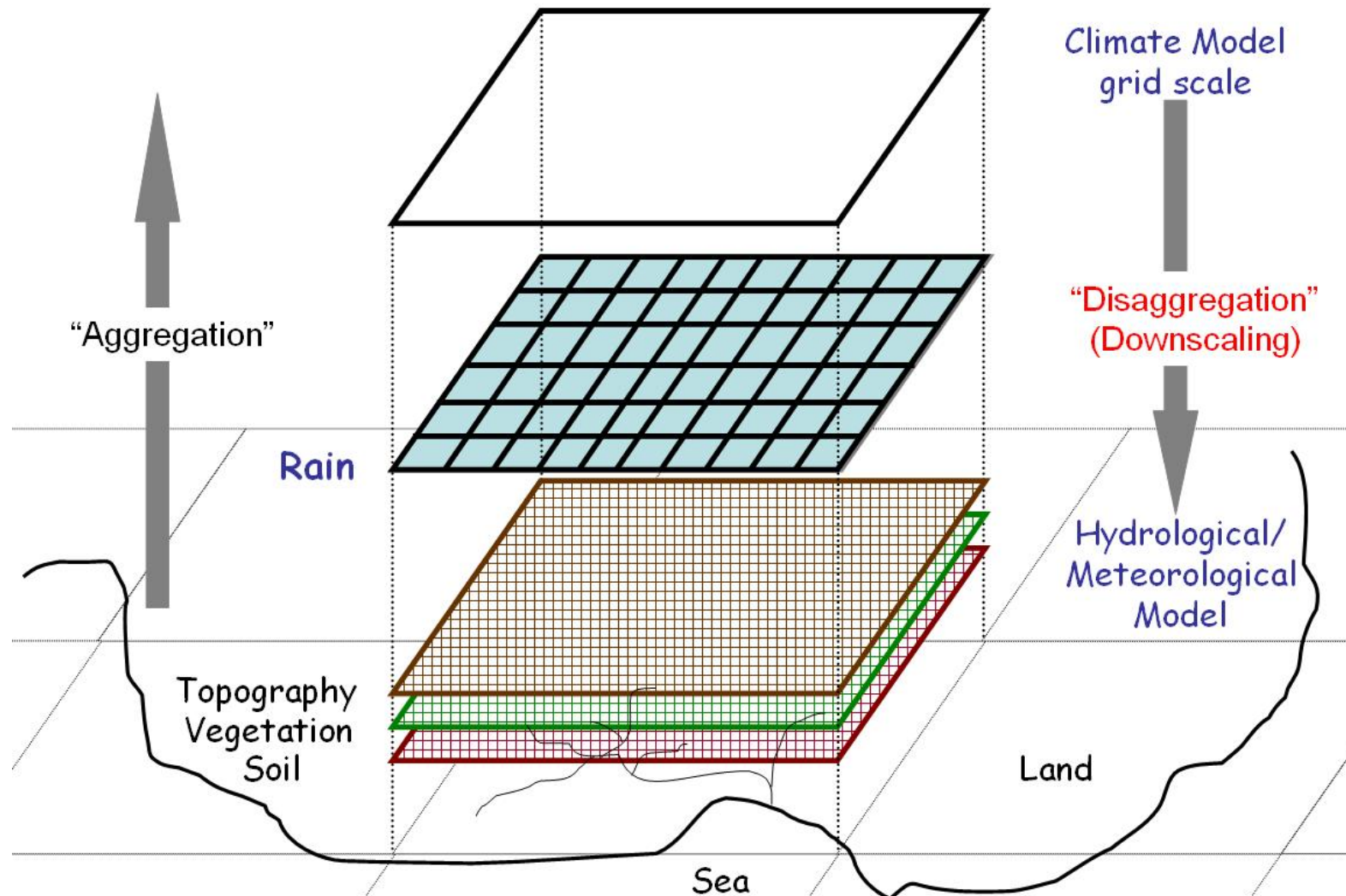


Space-time downscaling

(See Venugopal, Foufoula-Georgiou and Sapozhnikov, 1996)

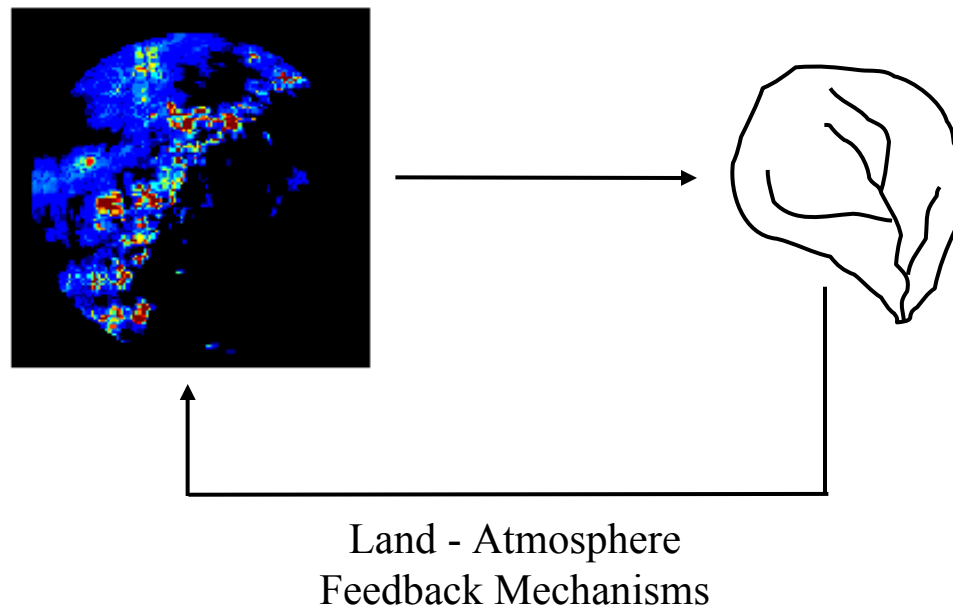


# 5. Hydrological Applications



# Effect of small-scale precipitation variability on runoff prediction

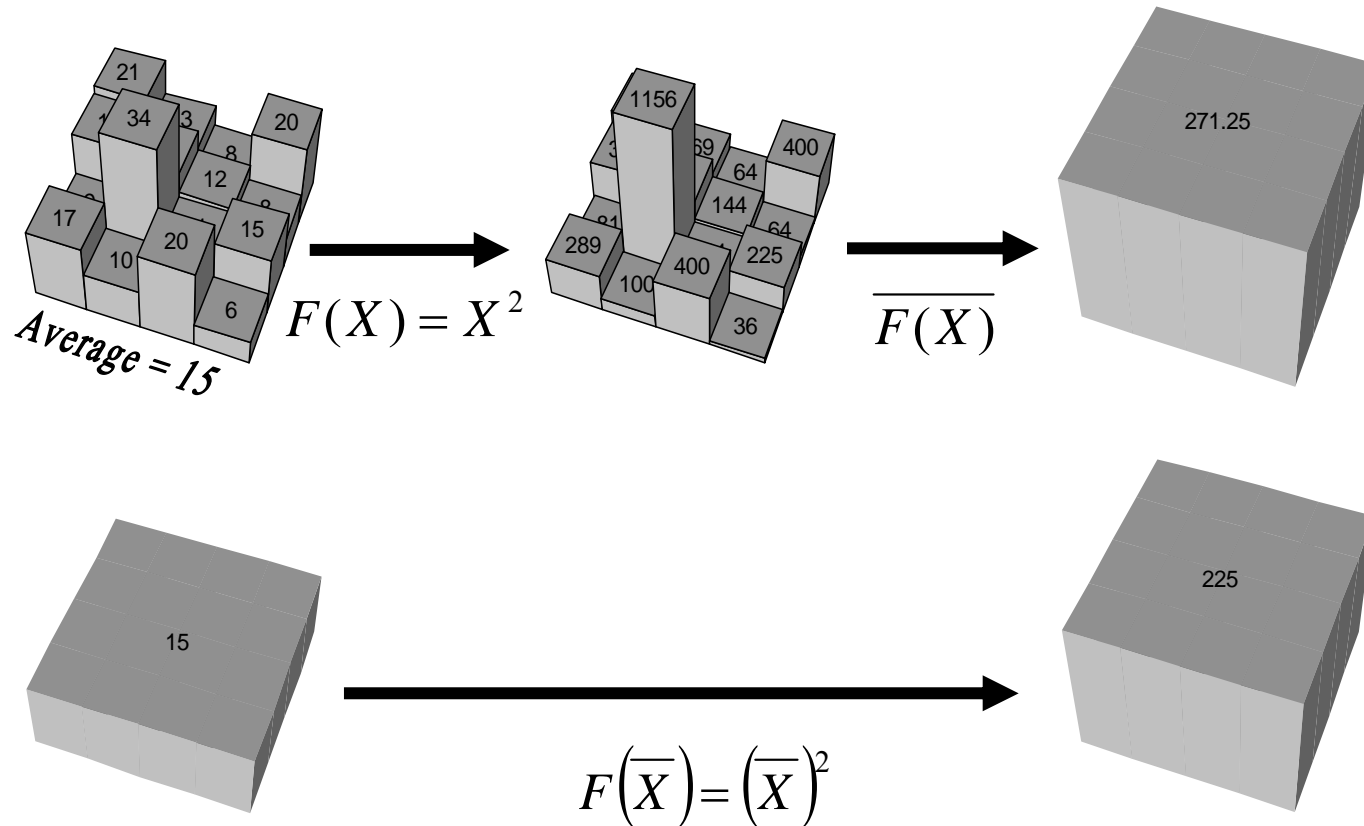
It is known that the land surface is not merely a static boundary to the atmosphere but is dynamically coupled to it.



Coupling between the land and atmosphere occurs at all scales and is nonlinear.

# Nonlinear evolution of a variable

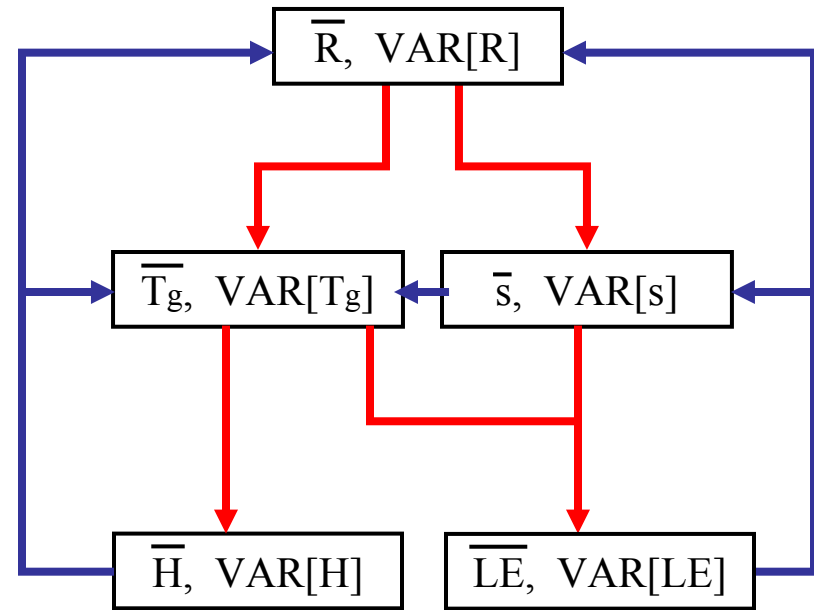
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$$\overline{F(X)} = \frac{1}{N} \sum_{i=1}^N F(X_i) \neq F(\overline{X})$$

- When subgrid-scale variability is introduced in the rainfall, it propagates through the nonlinear equations of the land-surface system to produce subgrid-scale variability in other variables of the water and energy budgets.

- Nonlinear feedbacks between the land-surface and the atmosphere further propagate this variability through the coupled land-atmosphere system.



Due to the nonlinearities of the **physical equations** and **feedback mechanisms** of the coupled land-atmosphere system, even the large-scale average values are effected (i.e.,  $\overline{F(X)} \neq F(\overline{X})$  ).

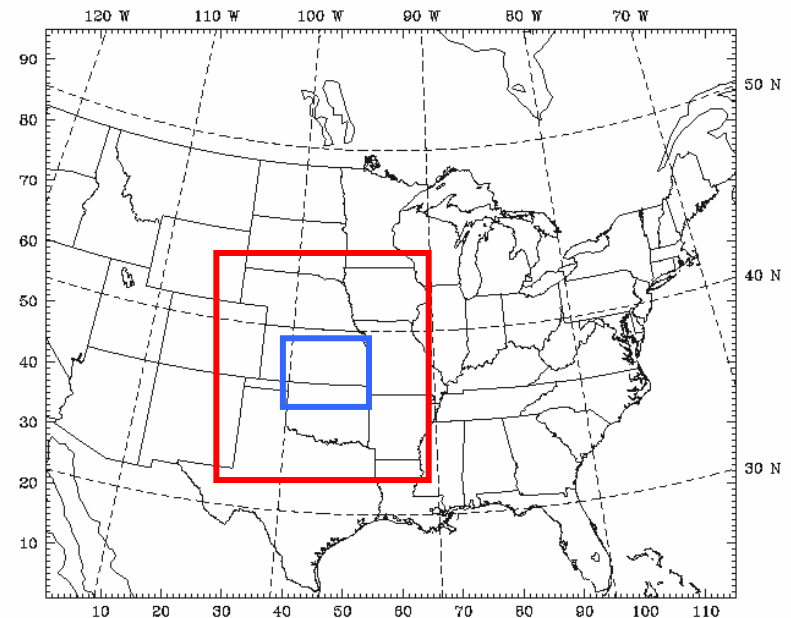
# Methods to account for small-scale variability in coupled modeling

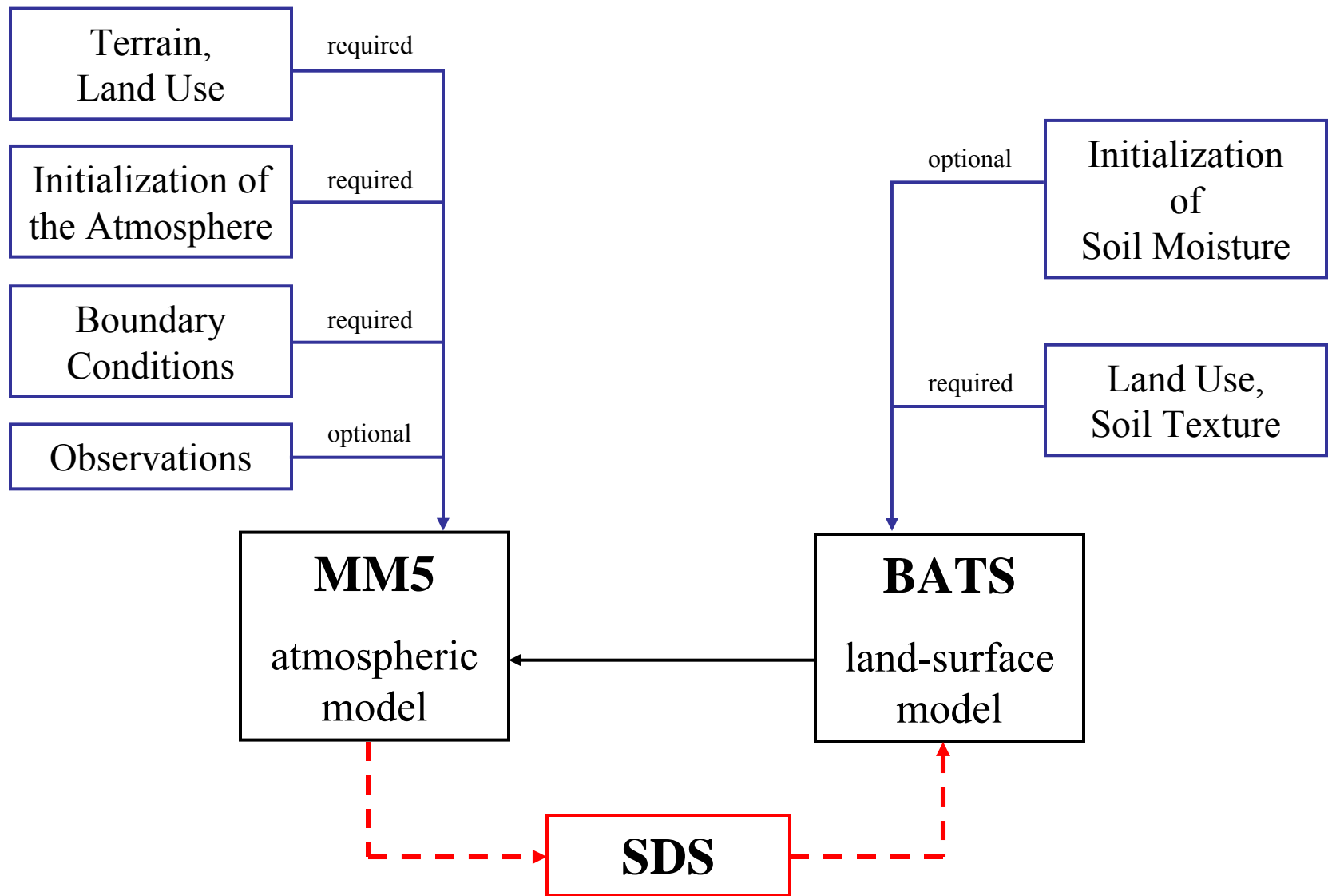
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(1) Apply the model at a high resolution over the entire domain.

(2) Use nested modeling to increase the resolution over a specific area of interest.

(3) Use a dynamical/statistical approach to including small-scale rainfall variability and account for its nonlinear propagation through the coupled land-atmosphere system.





Statistical Downscaling Scheme for Rainfall

(See Nykanen and Foufoula-Georgiou, 2001)



# Rainfall Downscaling Scheme

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(Perica and Foufoula-Georgiou, *JGR*, 1995)

→ It was found that for mesoscale convective storms, that normalized spatial rainfall fluctuations ( $\xi = X' / X$ ) have a simple scaling behavior, i.e.,

$$\frac{\sigma_{\xi, L_1}^{\xi}}{\sigma_{\xi, L_2}^{\xi}} = \left( \frac{L_1}{L_2} \right)^H$$

→ It was found that H can be empirically predicted from the convective available potential energy (CAPE) ahead of the storm.

→ A methodology was developed to downscale the fields based on CAPE  $\Rightarrow$  H.

# Simulation Experiment

- MM5: 36 km with 12 km nest
- BATS: 36 km with 3 km inside MM5's 12 km nest
- Rainfall Downscaling: 12 km → 3 km

Domain 1:

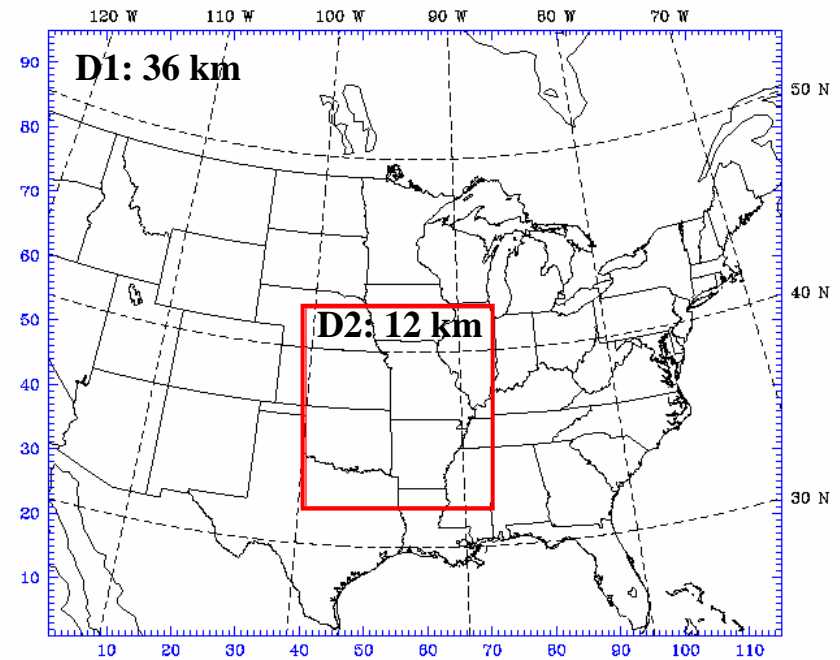
Run	MM5	BATS	Rainfall Downscaling
CTL	36 km	36 km	Off
SRV	36 km	36 km	Off

Domain 2:

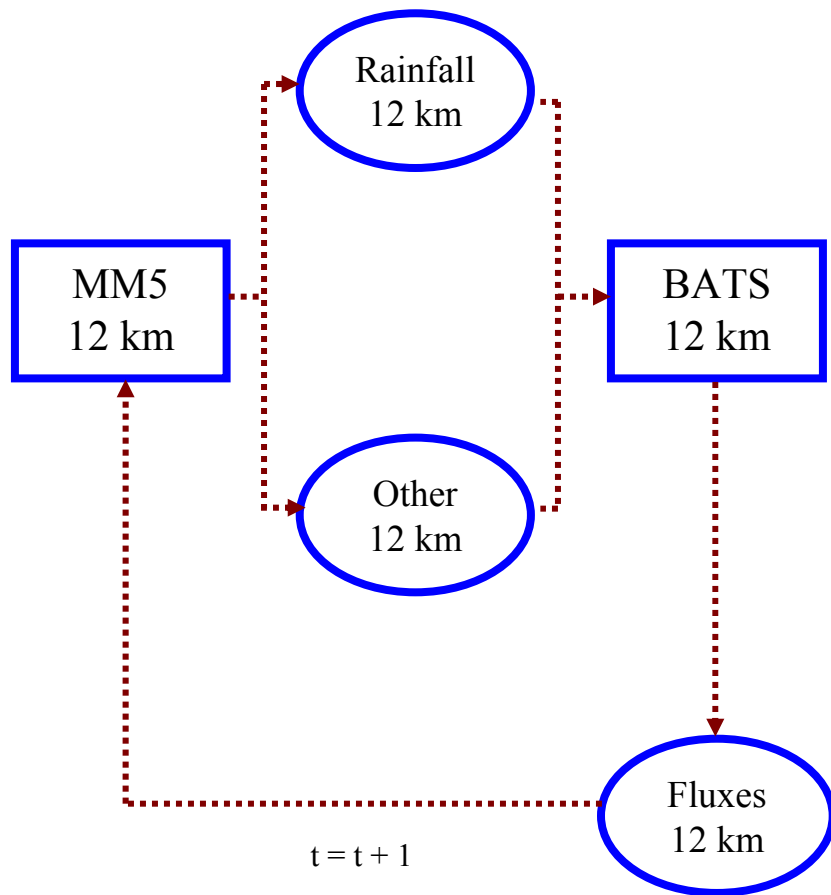
Run	MM5	BATS	Rainfall Downscaling
CTL	12 km	12 km	Off
SRV	12 km	3 km	12 km → 3 km

# Case Study: July 4-5, 1995

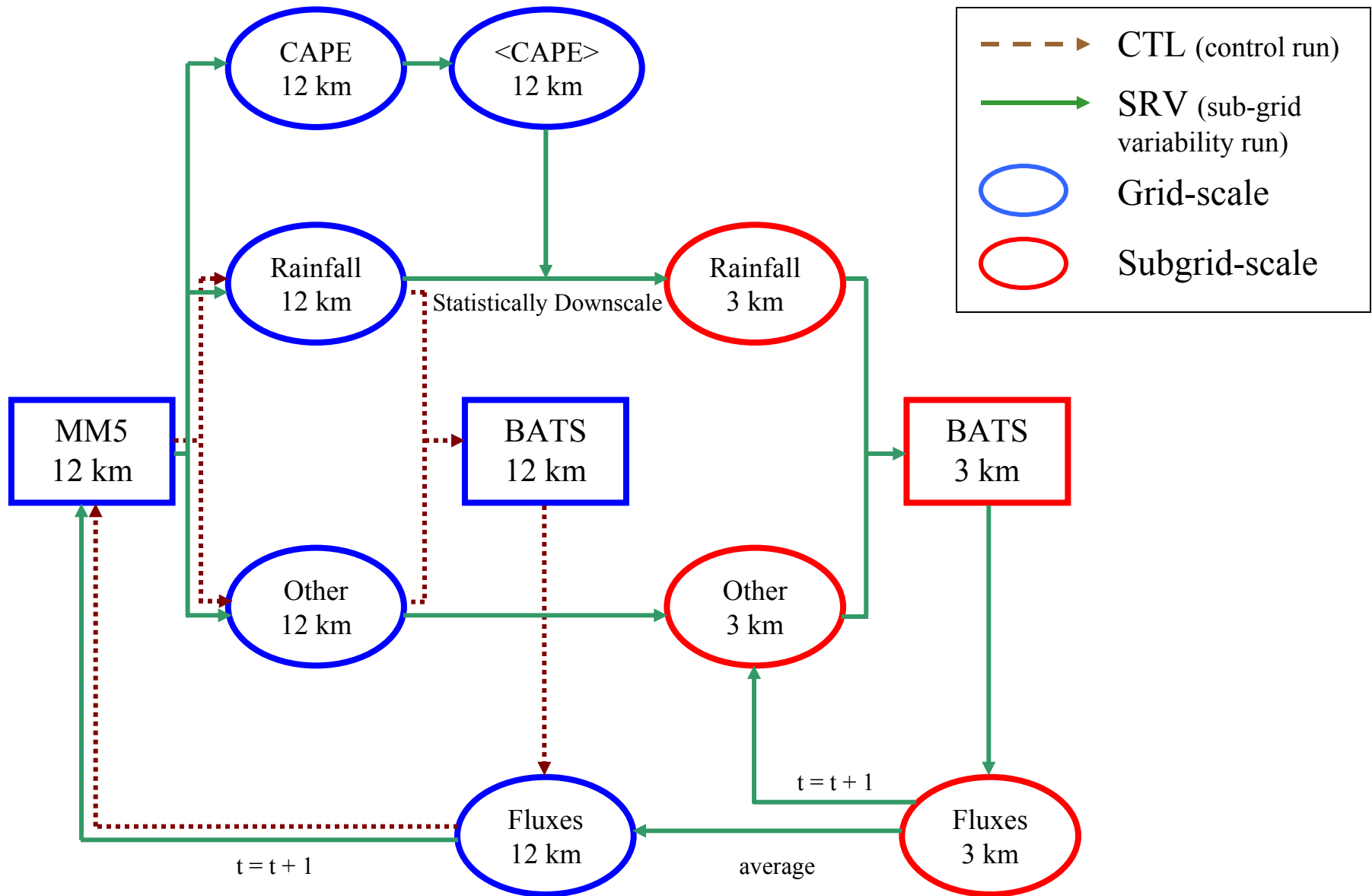
Initialization Time	July 4, 1995 12:00 UTC
Integration Time Step	D1: 90 sec., D2: 30 sec.
Simulation Length	48 hrs.
No. of Vertical Grid Elements	32
Horizontal Grid Resolution	D1: 36km, D2: 12 km
Initial and Lateral Boundary Conditions	NCEP Early Eta Model Analysis
Soil Moisture Initialization	Soil Hydrology Model (SHM) (via Penn State ESSC)
Land Cover, Soil Texture	USGS-EDC
Nesting Type	Two-way interactive
Cumulus Parameterization Scheme	Grell

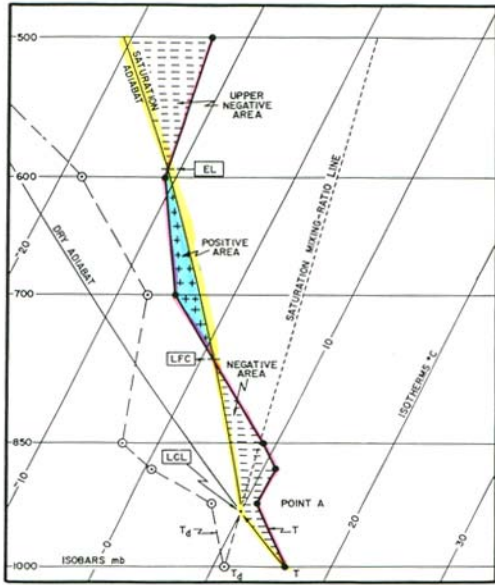


# MM5/BATS



# Subgrid-scale implementation of MM5/BATS

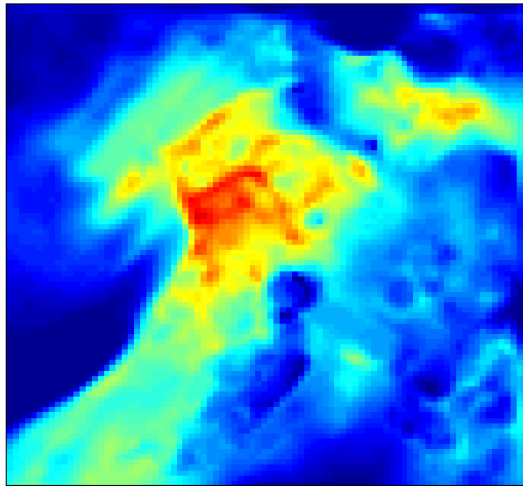




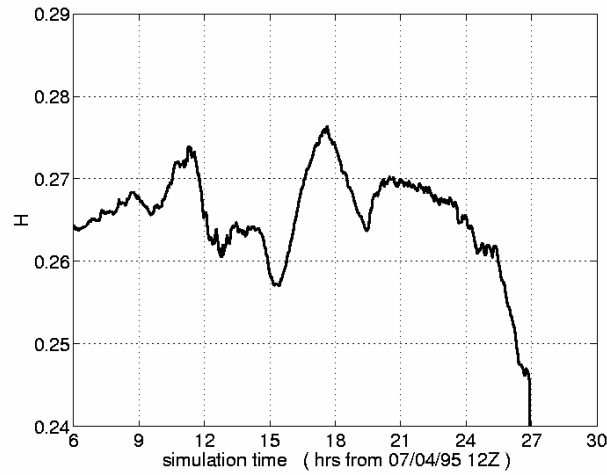
(adopted from AWS manual, 1979)

Yellow Line = Parcel  
 Pink Line = Environment  
 Positive Area = CAPE

CAPE (m<sup>2</sup>/s<sup>2</sup>) @ t = 9 hrs

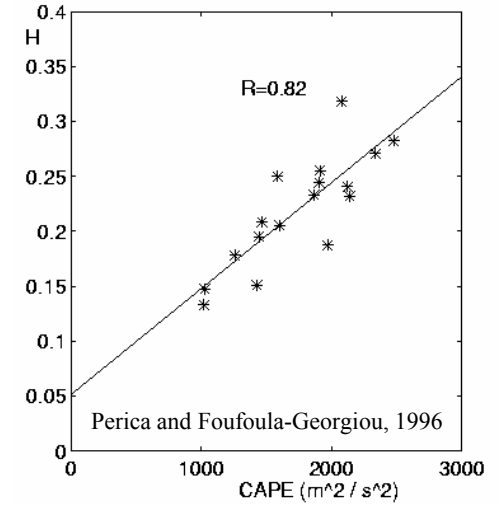


Domain 2 @ 12 km resolution

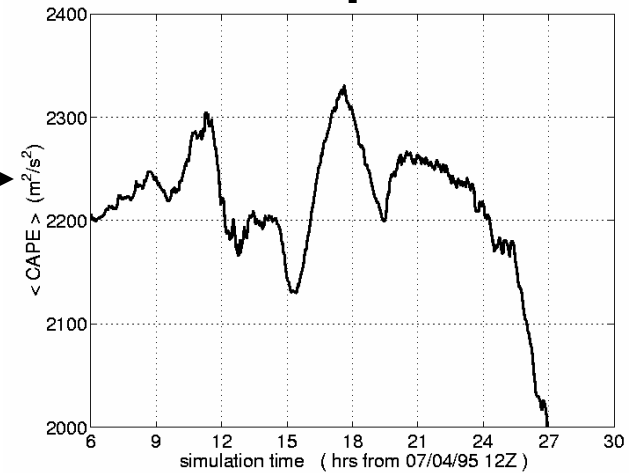


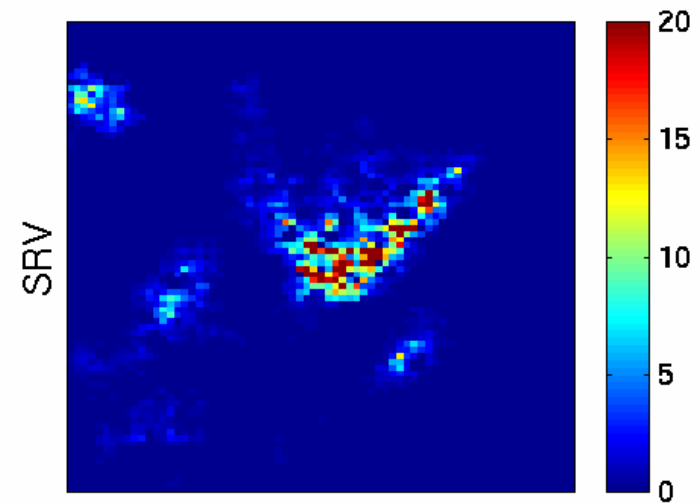
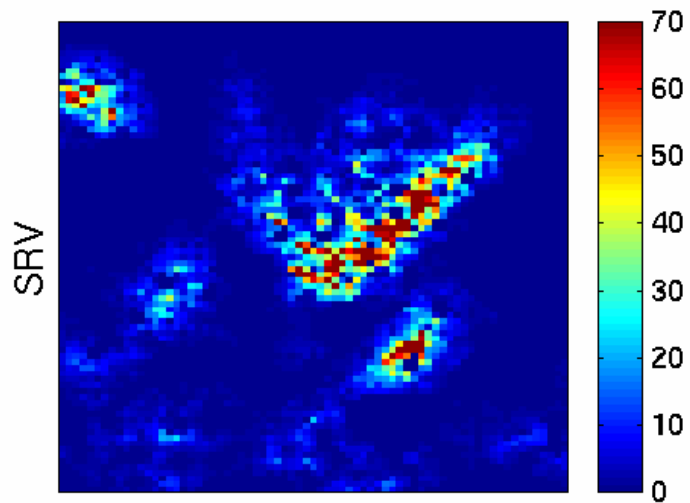
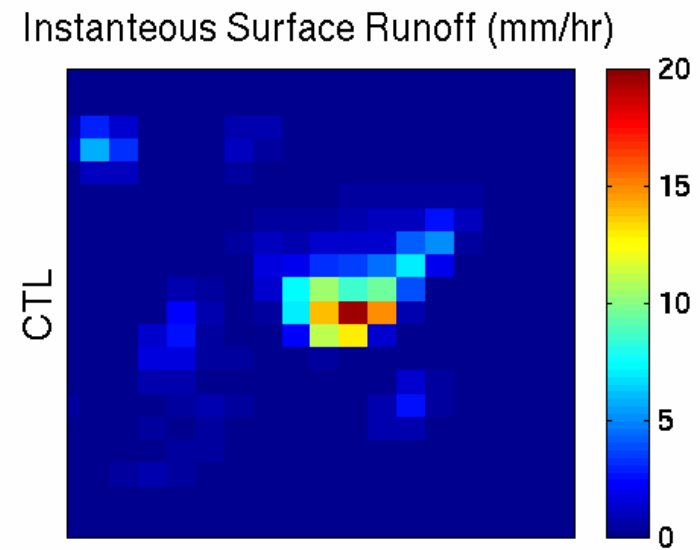
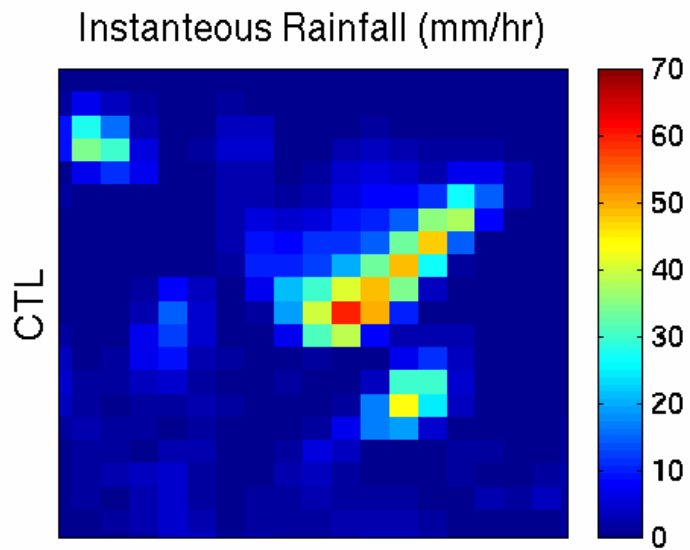
$$\frac{\sigma_{\xi, L_1}}{\sigma_{\xi, L_2}} = \left( \frac{L_1}{L_2} \right)^H$$

$$H = 0.052 + 0.965 \langle CAPE \rangle \times 10^{-4}$$



$$\langle CAPE \rangle = \frac{1}{N_s} \sum_{i=1}^N CAPE_i \times I_{K_s, i}$$





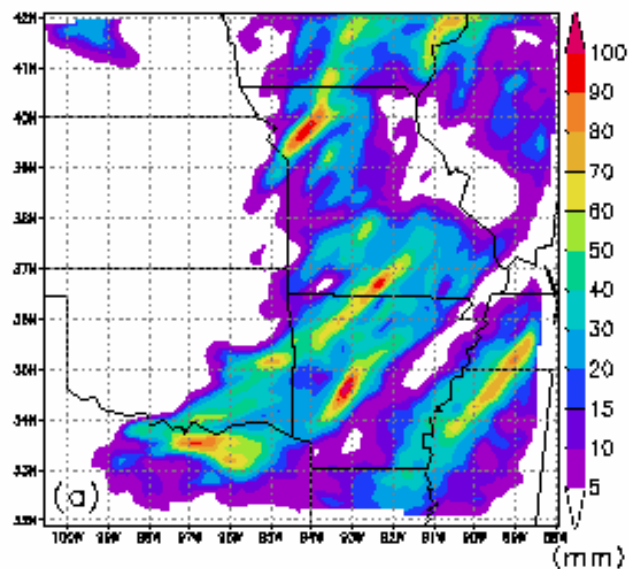
sub-domain @  $t = 11$  hrs, 20 minutes (680 minutes)

t = 27 hrs

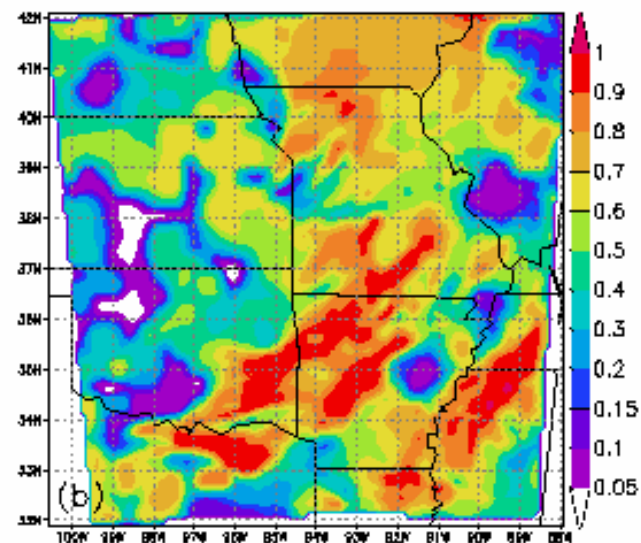
at 12 km  
grid-scale

CTL Run

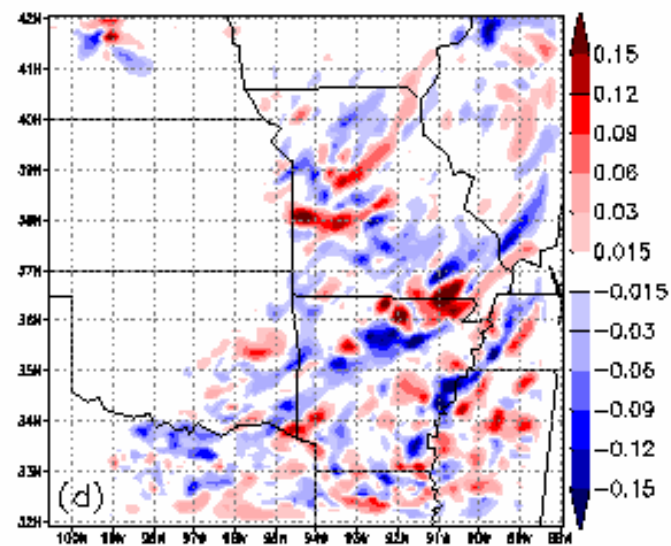
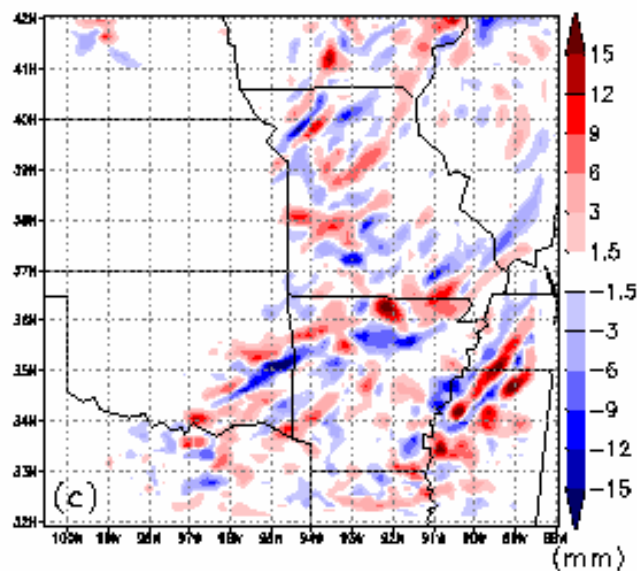
Total Accumulated Rainfall



Relative Soil Moisture in top 10 cm



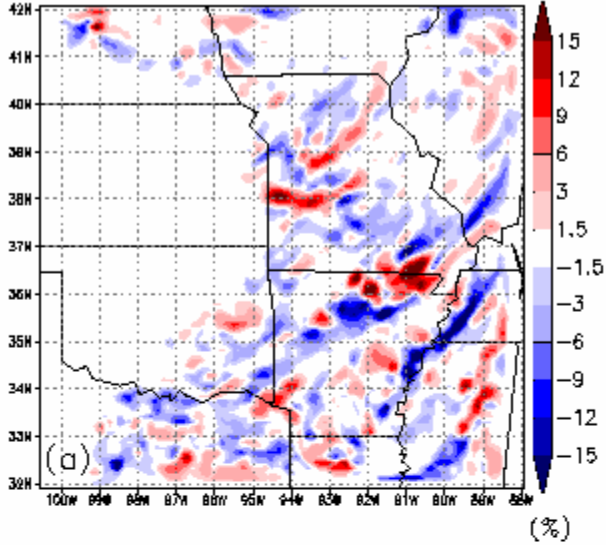
Anomalies  
(SRV - CTL)



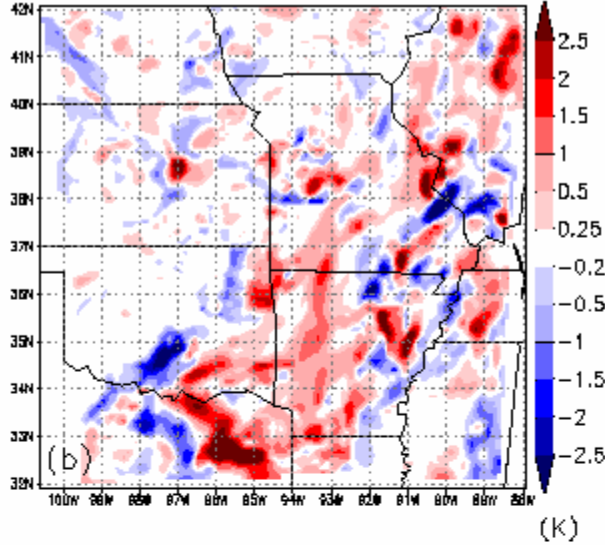
t = 32 hrs  
at 12 km  
grid-scale

$$\text{Anomalies} = \text{SRV} - \text{CTL}$$

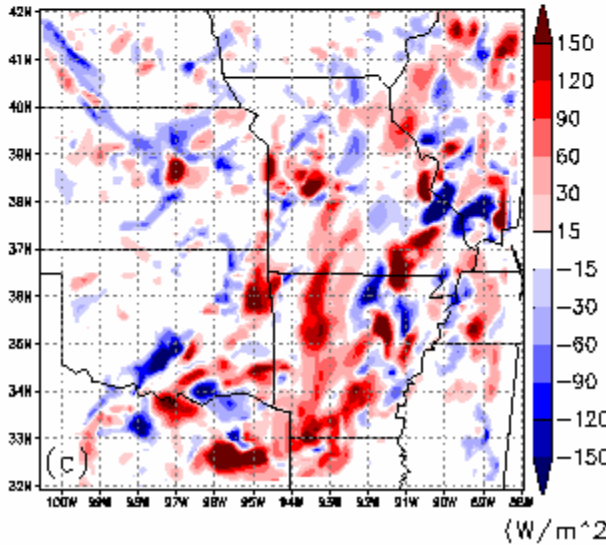
Relative Soil  
Moisture in  
top 10 cm  
( Su )



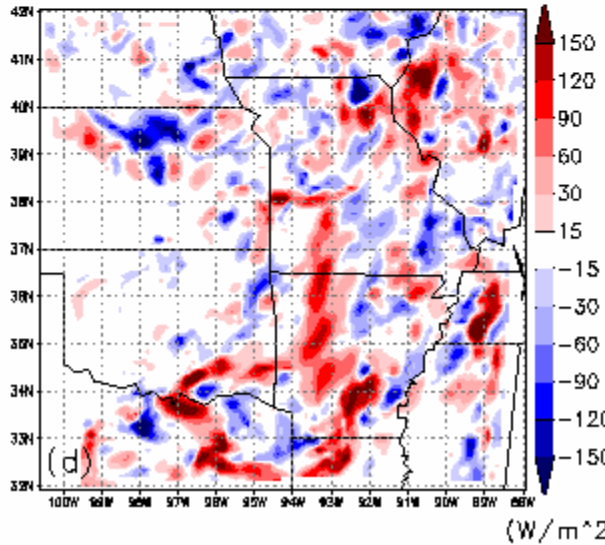
Surface  
Temperature  
( TG )



Sensible Heat  
Flux from the  
surface  
( HFX )



Latent Heat  
Flux from the  
surface  
( QFX )





# CONCLUSIONS

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- Statistical downscaling schemes for spatial and space-time precipitation are efficient and work well over a range of scales
- The challenge is to relate the parameters of the statistical scheme to physical observables for real-time or predictive downscaling
- The effect of small-scale precipitation variability on runoff production, soil moisture, surface temperature and sensible and latent heat fluxes is considerable, calling for fine-scale modeling or scale-dependent empirical parameterizations
- For orographic regions other schemes must be considered

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